

Multi-channel Digital Receiver Data Acquisition System for the Arecibo Radar

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Abstract

Digital Receivers are commercially available, cost effective solutions that are becoming commonplace in modern data acquisition systems (DAS). The digital receiver has the ability to be reconfigured via software, making modern DAS flexible for a variety of applications. This thesis describes the design and implementation of a complete data acquisition system using a general purpose computer (GPC) equipped with a digital receiver card. This system will replace the older DAS (baseband sampling) used by the Space and Atmospheric Science (SAS) group at the Arecibo Observatory (AO). Emphasis is placed on a generic system easily adaptable to a specific application with minimal effort. A full discussion of the system will be given with concentration on the receiver's capabilities and software design. Algorithms and design strategy are discussed to properly document optimizations and features required by the system. Finally, we present two radar observations with this system and illustrate results.

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List of Abbreviations

1. ADC Analog to Digital Converter
2. AO Arecibo Observatory
3. ASIC Application Specific Integrated Circuit
4. CIC Cascaded Integrator Comb Filter
5. COTS Commercial off-the-shelf
6. DAS Data Acquisition System
7. DDC Digital DownConverter
8. DFT Discrete Fourier Transform
9. DNL Differential Non-Linearity
10. DSP Digital Signal Processing
11. FFT Fast Fourier Transform
12. FIR Finite Impulse Response
13. GPC General Purpose Computer

14. IC Integrated Circuit
15. IF Intermediate Frequency
16. IIR Infinite Impulse Response
17. INL Integral Non-Linearity
18. IPP Inter-Pulse Period
19. LSB Least Significant Bit
20. LTI Linear Time Invariant Systems
21. NCO Numerically Controlled Oscillator
22. OOD Object Oriented Design
23. OOP Object Oriented Programming
24. OSR OverSampling Ratio
25. SDR Software Defined Radio
26. UML Unified Modeling Language

Chapter 1

Introduction

Motivation for this work is to explore the use of commercial off-the-shelf (COTS) digital receivers, commonly used in Software Defined Radio (SDR) architectures, for use in modern data acquisition systems (DAS); and, in this specific application, space and atmospheric research at the Arecibo Observatory (AO). In the past, traditional receiver architectures implemented a superheterodyne architecture combined with digitization at baseband. In contrast, modern digital receiver architectures sample at intermediate frequencies (IF). This key difference reduces the receiver architecture's complexity and lessens analog component specifications while removing gain and phase imbalances found in analog quadrature mixers. Advances in semiconductor technology are slowly moving the receiver's digitization point closer to the receiver's front-end. Currently, digital receivers are capable of digitizing data at intermediate frequencies (IF) and, depending on the system, RF sampling is a possibility. Modern DAS [23, 14], the focus of this thesis, encompass both back-end digital receivers and general purpose computers (GPC). The combination of both digital receiver and GPC form the basis of a modern DAS which typically perform three tasks: 1) digitization, or sampling of analog signal(s), 2) digital

signal processing (DSP), 3) formatting and storage of data. The remainder of this chapter will provide an overview of techniques related to radar operation, signal processing, and software design required for the discussion of modern DAS; which is the central topic of this thesis. In Chapter 2, an in-depth study of the system's internals, including the digital receiver hardware and software is presented. Chapter 3 will illustrate data from multiple radar observations. Finally, conclusions and future work are discussed in Chapter 4.

1.1 Radar Techniques

Backscatter radars operate in both transmit and receive modes by isolating each mode using mechanical (duplexer) or electrical (T/R switch) devices as shown in Figure 1.1. These type of radars transmit short, periodic waveforms $p(t)$ with a duty cycle

$$\frac{\delta(t)}{T}, \tag{1.1}$$

where $\delta(t)$ is the transmitter pulse width and T is the period; (1.1) is also called the interpulse period (IPP). The complete transmitted signal of the radar

$$s(t) = p(t)e^{j\omega_0 t} \tag{1.2}$$

is a combination of the modulating waveform $p(t)$ and a carrier frequency $e^{j\omega_0 t}$. In receive mode, backscatter radar returns are sampled by the radar receiver for further analysis. The sampled signal $\alpha s(t - 2r/c)$ is returned from a radar target at range r as depicted in Figure 1.2.

Ionospheric plasma-density irregularities are typically observed with pulsed backscatter radars that operate at twice the wavelength of ionospheric density fluctuations. Only

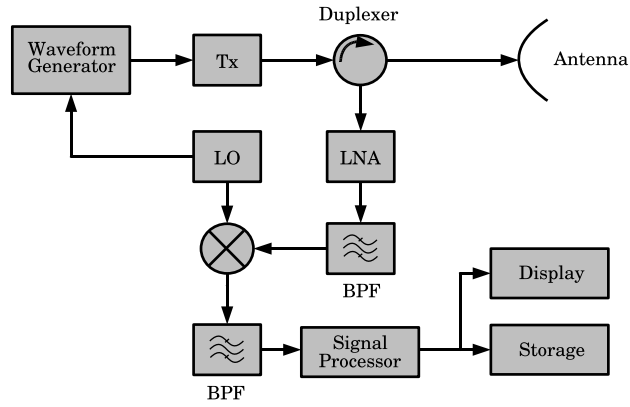


Figure 1.1: Backscatter Radar Layout

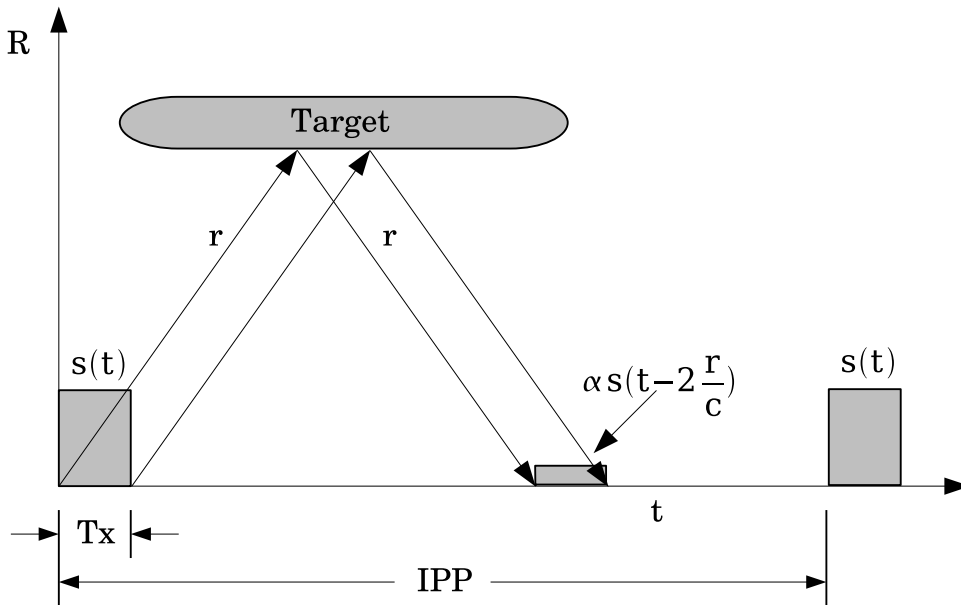


Figure 1.2: Range Time Diagram

very large power/aperture product radars, known as incoherent scatter radars (ISR) (e.g. the Arecibo radar), can detect density fluctuations in a stable ionosphere. These radars are powerful remote sensing tools to study the ionosphere in equilibrium. A simplified

model of the average received power ($\langle P_r \rangle$) in an ISR experiment is described by

$$\langle P_r \rangle = \eta P_t \frac{A_{max} \delta R}{4\pi R^2} \sigma \tilde{N}, \quad (1.3)$$

where η is the system calibration factor (that takes into account ohmic losses, etc), P_t is transmitted power, σ is backscatter radar cross section of a free electron, \tilde{N} is the average electron density, R is the radar range, A_{max} is the effective area of the radar antenna, and δR is the range resolution [10].

1.2 Radar Receivers

In general, a radar receiver performs the following tasks: 1) detect and isolate a desired signal in the presence of noise, 2) translate the signal into a format compatible with the system, and 3) digitize the signal for further processing.

In radar systems, the antenna is sensitive to the desired RF signals and largely determines the signal-to-noise ratio (SNR) of the detected signal. After detection, filtering and amplification isolate the desired signal from unwanted noise and the signal's spectral content is down-shifted to alleviate physical limitations in the processing chain. Combination of these processes define a receiver's topology and many topologies exist [14, 23], with each providing unique characteristics. Of these, the superheterodyne architecture is commonly used due to many advantages including: 1) amplifier and filter requirements are lessened, 2) decoupling of the front- and back- ends, and 3) components are widely available for standard intermediate frequencies (IF). This architecture uses one or more stages of down-conversion to shift the signal down to a specified IF. In the analog domain,

the down-conversion process is a multiplication of two signals

$$y(t) = s_{LO}(t)s_m(t), \quad \text{where}$$

$$s_{LO}(t) = e^{-j\omega_{LO}t}$$

$$s_m(t) = A_m(t)e^{j\omega_{LO}t+\theta_m(t)}.$$

A graphical representation is shown in Figure 1.3. Combination of the superheterodyne

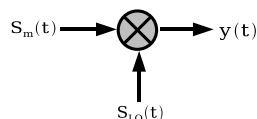


Figure 1.3: Signal Mixer

architecture and analog quadrature mixing for baseband conversion are key features of a traditional radar receiver. In this configuration, quadrature down-conversion translates the IF signal to baseband while preserving both amplitude and phase, which are required for coherent sampling. An overview of the traditional radar architecture is illustrated in Figure 1.4.

A modern form of radar receiver samples the IF signal allowing quadrature down-conversion in the digital domain; these receivers are labeled digital receivers and the general topology is depicted in Figure 1.5. Sampling IF signals enable systems to employ a technique known as bandpass sampling [24] in addition to nyquist sampling used in traditional receivers. The primary difference between the digital and traditional architectures is the position of the down-converting mixers; consequently, this detail defines the two architectures. The digital receiver digitally down-converts an IF signal using a Digital Down-Converter (DDC). The DDC [1] provides superior performance to conven-

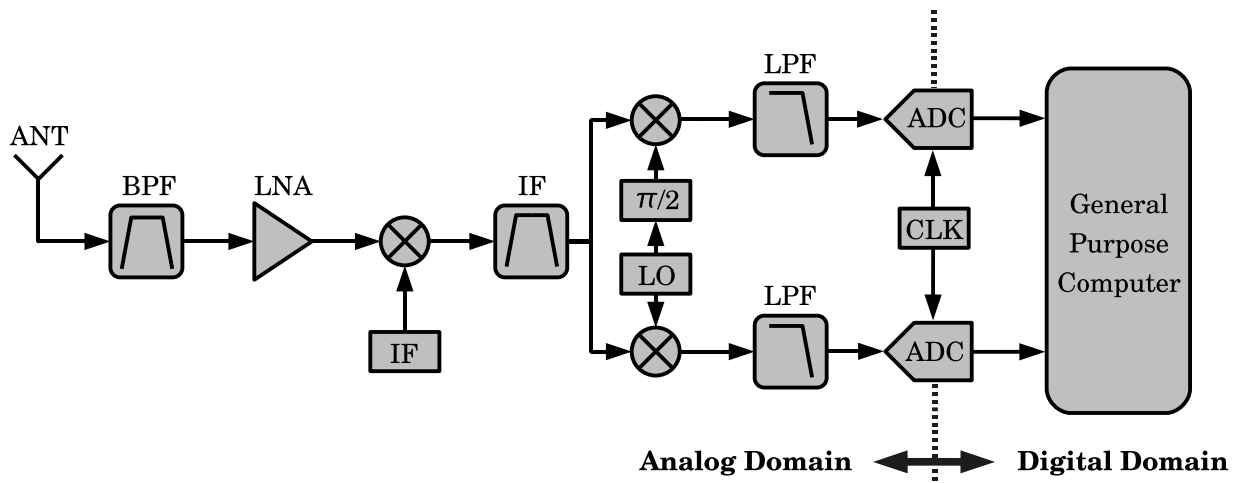


Figure 1.4: Superheterodyne Analog Receiver with Quadrature mixing

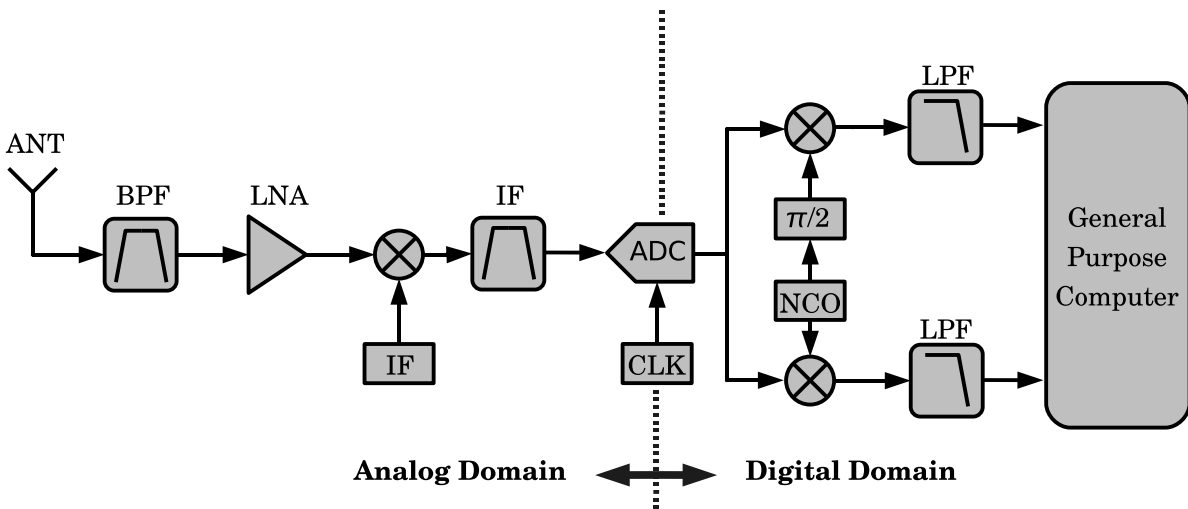


Figure 1.5: Superheterodyne Digital Receiver with Quadrature mixers

tional analog mixers; eliminating nonlinear effects and mismatch errors in seen in analog quadrature systems. The DDC creates a digital sinusoidal sequence for mixing using an N-bit programmable numerically controlled oscillator (NCO) as shown in Figure 1.6 This particular implementation is composed of the following components: 1) phase accumulator and 2) sine/cosine lookup table (LUT). Phase accumulators enable precise frequency

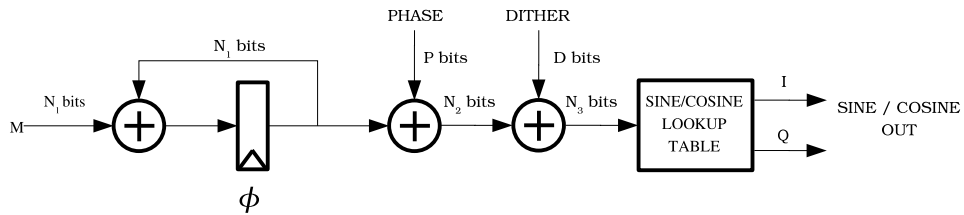


Figure 1.6: Numerically Controlled Oscillator

tuning, typically with sub-hertz resolution. Accumulation of phase, via feedback, is best described using a digital phase wheel as shown in Figure 1.7. The phase wheel contains

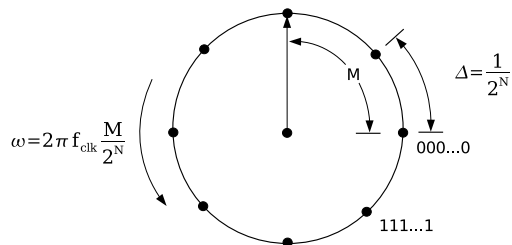


Figure 1.7: N-bit Digital Phase Wheel

a vector rotating counter-clockwise (CCW) at a rate f_{out} determined by

$$f_{out} = f_{clk} \frac{M}{2^N}, \quad (1.4)$$

where M is the tuning word, N is the bit resolution, and f_{clk} is the input clock rate. As the vector rotates, a linear sum is produced at the output. A static phase offset is programmed using a P – bit phase word. In order to reduce storage requirements, bit reduction, or phase truncation is needed. For example, a 32-bit accumulator would require a minimum storage of 2^{30} entries; and, when combined with the precision of the entry, total storage could exceed 1 GB. Notice that phase truncation, depending

on variables chosen in (1.4), can produce periodic phase errors [9, 22]. These periodic errors concentrate power in the frequency spectrum and are known as frequency spurs. Phase dithering is a technique commonly used to alleviate spurs by injecting random noise into the truncated phase sequence. This technique spreads spectral energy over the frequency band, resulting in an increase in the overall noise floor while reducing spur levels. In the final step, a sinusoidal waveform is generated using a LUT. After the down-conversion, data is generally filtered and resampled using a combination of DSP techniques implemented in hardware.

1.3 Digital Signal Processing

In recent years digital signal processing has gained significant approval and widespread acceptance in electronic design. Advances in semiconductor technology have made this possible by reducing component size and increasing speed. These advances have allowed digital technology to more accurately process signals that have been handled by analog processing systems in the past. Advantages over analog processing units include: 1) software reconfigurable hardware, 2) reduced cost and size, and 3) increased accuracy. The following sections describe concepts needed for implementation and design of a modern DAS.

1.3.1 Analog-to-Digital Conversion

A signal, by definition, is a detectable energy used to carry information which is encoded through temporal or spatial variations. Observation of physical processes in nature are converted, via sensors, into detectable signals via electrical current and a conductive transmission medium. The signal's information is revealed through signal processing

techniques. Since the advent of digital computers, signal processing and data storage techniques typically operate in the digital domain; drastically improving performance while decreasing storage requirements. Digital sampling is a process of transforming a continuous signal into a discrete sequence; this process is achieved through an analog-to-digital converter (ADC) chip. The operation performed by the ADC can be viewed as a process consisting of three steps: 1) sampling, 2) quantization, and 3) encoding of the signal. The first step of the conversion - sampling, performs the continuous to discrete conversion. For example, a pure analog sinusoid is described by

$$s_a(t) = A \sin(2\pi Ft + \phi) \equiv A \sin(\Omega t + \phi), \quad (1.5)$$

where the sub-notation a denotes an analog signal, A is the amplitude, F is frequency in hertz (Hz), Ω is angular velocity in radians per second (rad/s), and ϕ is the phase constant. Discussion is limited to *uniform sampling* which are samples taken at equidistant points with respect to time. The number of samples required to adequately represent a continuous waveform is given by Nyquist's theorem [20]

$$F_s \geq 2B, \quad (1.6)$$

where F_s is the sampling rate and B is the signal's bandwidth. A discrete version of (1.5) is given by

$$s_a(nT) = A \sin(\Omega nT + \phi_n), \quad (1.7)$$

where n is the sample number and T is the sample period. Both forms are illustrated in Figure 1.8. The sample period is inversely related to the sample frequency $F_s = 1/T$ with units of samples per second (SPS). The ratio of continuous frequency to sampled

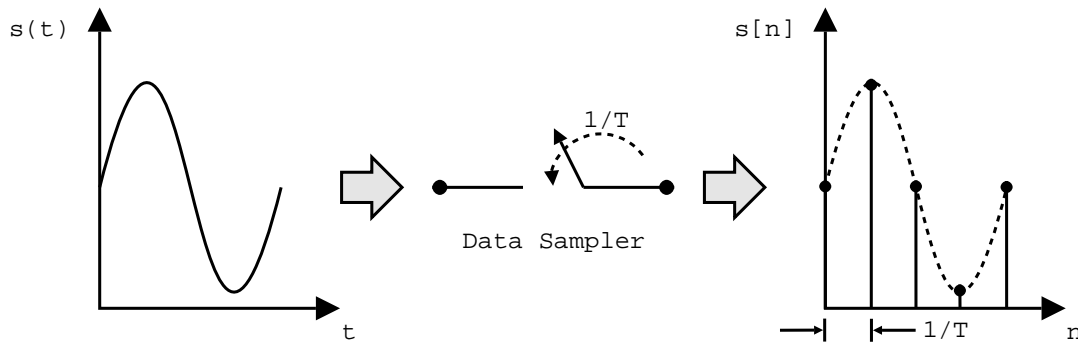


Figure 1.8: Digital Sampling

frequency, is

$$s_a(nT) = A \sin\left(2\pi \frac{F}{F_s} n + \phi_n\right) \equiv A \sin(2\pi f n + \phi_n) \equiv A \sin(\omega n + \phi_n), \quad (1.8)$$

where f is normalized frequency, and ω is angular velocity in samples per second (SPS).

A shortened notation

$$s[n] \equiv s_a(nT) \quad (1.9)$$

is adopted in most modern texts and will be used in this thesis to represent discrete samples.

After sampling, each sample in the sequence contains a numerical representation of the signal's energy level at a single, instantaneous point in time. In practice, resolution of the sampled sequence is rounded or truncated due to the limited number of bits in the ADC, and this introduces an error into the sampled sequence known as quantization. Signal quantization can be viewed as a non-invertible transformation of the original, sampled

sequence. Quantization is described by

$$x_q[n] = Q \left[x[n] \right], \quad (1.10)$$

and the resulting error is

$$e_q[n] = x_q[n] - x[n]. \quad (1.11)$$

A simple two-level rounding quantizer is illustrated in Figure 1.9. Assuming a rounding

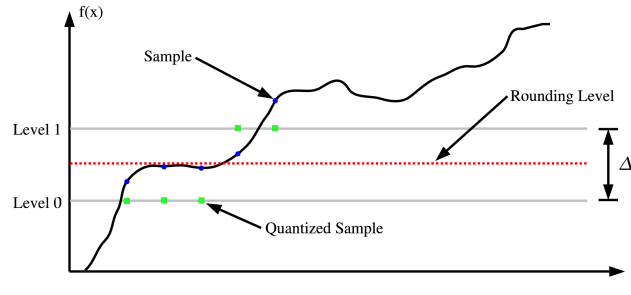


Figure 1.9: 2 level quantization

quantizer, the maximum error is $\max(e_q[n]) = \pm\Delta/2$, where Δ is the step size of the conversion and the Least Significant Bit (LSB) of the sample is

$$LSB \equiv \Delta = \frac{V_{range}}{2^b}, \quad (1.12)$$

where b = bit resolution of the ADC. To analyze effects due to quantization noise, a statistical approach is taken, and the following assumptions are made [13]:

1. The error is uniformly distributed over the range $-\frac{\Delta}{2} \leq e \leq \frac{\Delta}{2}$
2. The error sequence is a stationary white noise sequence.
3. The error sequence is uncorrelated with the signal sequence.

4. The signal sequence is zero mean and stationary.

The probability density function (pdf) of the error signal is defined as

$$p(e) = \begin{cases} \frac{1}{\Delta} & -\frac{\Delta}{2} \leq e \leq \frac{\Delta}{2} \\ 0 & \text{elsewhere} \end{cases} \quad (1.13)$$

and an illustration is provided in Figure 1.10 The mean-square noise power is

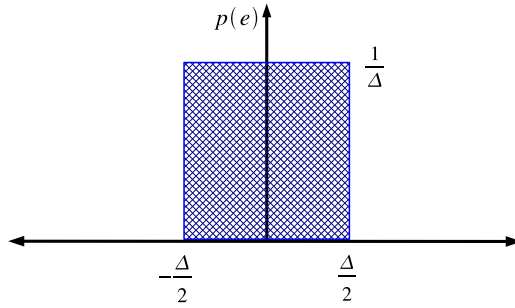


Figure 1.10: noise probability distribution

$$P_n \equiv \sigma_e^2 = \int_{-\frac{\Delta}{2}}^{\frac{\Delta}{2}} e^2 p(e) de = \frac{1}{\Delta} \int_{-\frac{\Delta}{2}}^{\frac{\Delta}{2}} e^2 de = \frac{\Delta^2}{12}. \quad (1.14)$$

The Signal to Quantization Noise Ratio (SQNR) provides a comparison of signal power vs. noise power due to quantization

$$SQNR = 10 \log \left(\frac{P_x}{P_n} \right) = 20 \log \left(\frac{\sigma_x}{\sigma_e} \right); \quad (1.15)$$

this equation reduces to

$$SQNR = 10.79 + 6.02b + 10 \log(FFS), \quad (1.16)$$

where FFS is the percentage of the full scale value of the input signal. A model commonly used to simulate statistical quantization effects is illustrated in Figure 1.11. This model is sufficient when the quantization level Δ is small and the randomness of the signal spans multiple levels between samples.

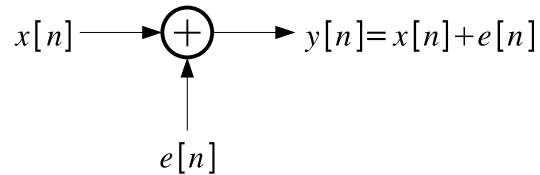


Figure 1.11: quantization error model

Data Encoding is the final step in the ADC process. Digital logic imposes limitations on numerical representations that must be taken into account when designing DSP systems. Any real number can be represented digitally using a finite word length, placing constraints on numerical precision and introducing nonlinearity to the system [5]. Negative number formatting must also be accounted for since digital logic representations use only '1's and '0's. Fixed point representation of a number provides a general notation for representing numbers using decimal notation. In this notation, any real number is given by

$$r = \pm \left[\sum_{j=0}^n b_j \beta^j + \sum_{k=1}^p \frac{f_k}{\beta^k} \right], \quad (1.17)$$

where n represents the integer contribution, p represents the fractional portion, and β is the base. Together, both n and p in (1.17) can be adjusted to provide the precision. Digital numerical representations commonly use a base of 2, known as the binary number system. A variety of numerical representations exist [5] but 2's complement format is the

most commonly used

$$k = -b_n 2^n + \sum_{j=0}^{n-1} b_j 2^j, \quad (1.18)$$

where b_n is the sign bit

$$b_n = \begin{cases} 0 & k \geq 0; \\ 1 & k < 0. \end{cases} \quad (1.19)$$

Figure 1.12, using a 3-bit integer, depicts a graphical notation of the 2's complement format and emphasizes 2's complement unique overflow behavior. Finally, the quantized,

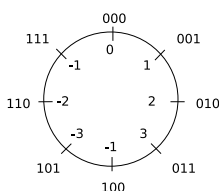


Figure 1.12: 3-bit two's complement integer representation

encoded sample is available at the output of the ADC for further processing.

1.3.2 Discrete Time Systems

Operations on discrete-time signals are characterized by discrete-time systems which transform an input sequence into an output sequence

$$y[n] = \tau \left[x[n] \right], \quad (1.20)$$

where $\tau[\cdot]$ is the system transform operator. Block diagrams, as shown in Figure 1.13, are useful when describing behavior of large systems. Algorithms used in transformations

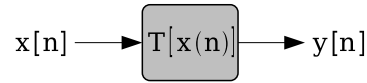


Figure 1.13: Discrete Time System

are described graphically using a small set of operations shown in Figure 1.14. When combined, these operations are capable of defining any system, regardless of complexity. Discrete-time systems are classified according to properties they possess. A special class

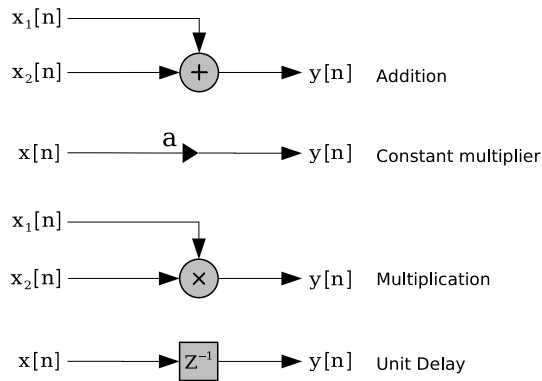


Figure 1.14: Basic System Operations

of systems known as linear time-invariant systems (LTI) are commonly used to develop an understanding of DSP theory. System linearity is defined by properties of homogeneity and additivity.

1. Homogeneity: Scaling the input sequence will result in an equal scaling of the output sequence.

$$y[t] \equiv \tau [kx[n]] = k\tau [x[n]]$$

2. Additivity: An output response due to a summation of input sequences is equivalent to a sum of the output response of each individual input sequence.

$$y[t] \equiv \tau \left[x_1[t] + x_2[t] \right] = \tau \left[x_1[t] \right] + \tau \left[x_2[t] \right]$$

Time-invariance is used to describe a system with no dependence on time and is expressed by

$$y[n - k] = \tau \left[x[n - k] \right]. \quad (1.21)$$

Combination of these two principles define the LTI system and this system is completely defined by its impulse response in an operation known as the convolution sum

$$y[n] = \sum_{k=0}^{k=\infty} h[k]x[n - k]. \quad (1.22)$$

Systems employing digital filtering techniques make use of (1.22) and two types of digital filters exist:

1. Finite Impulse Response (FIR) Filter: This filter provides stability and linear phase response due to its finite response $h[n]$.
2. Infinite Impulse Response (IIR) Filter: These filters are used due to their efficient, recursive structure.

Of the two filter types, focus is given to FIR filters and interested readers are directed to [15, 17, 18, 13] for further reading.

1.3.3 Multirate Systems

Decimation, or down-sampling of a signal, is a process in which the sampling rate is reduced by an integer factor D . To prevent aliasing, a filter is typically used to limit bandwidth to the Nyquist rate of the decimated sampling rate. To illustrate this concept, imagine a signal with a frequency response shown in Figure 1.15. If the original sample

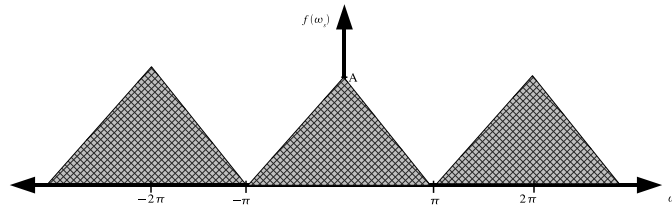


Figure 1.15: Image bandwidth

rate were ω_s , the decimated sample rate becomes $\omega_D = \omega_s/D$. To prevent aliasing at the down-sampled rate, a filter with frequency response

$$H_D(\omega) = \begin{cases} 1 & -\frac{\pi}{D} \leq \omega \leq \frac{\pi}{D} \\ 0 & \text{elsewhere} \end{cases} \quad (1.23)$$

is required. This filter is shown in Figure 1.16. After filtering, decimation reduces image

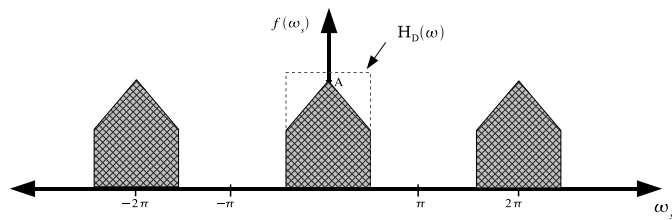


Figure 1.16: Decimation Image Filter

separation resulting from sample rate reduction and Figure 1.17 illustrates this concept.

A block diagram of this filter is shown in Figure 1.23. where $v[n]$ is the convolution sum

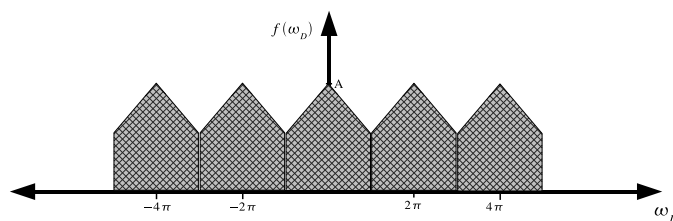


Figure 1.17: Resulting spectrum from decimation

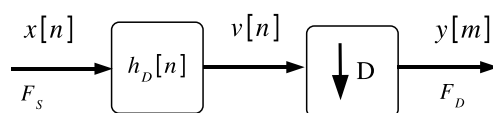


Figure 1.18: Decimation Block Diagram

of the input sequence with the unit sample response of the filter.

$$v[n] = \sum_{k=0}^{\infty} h[k]x[n - k]. \quad (1.24)$$

The result in Equation (1.24) is decimated by D producing the output $y[m]$, where m represents the decimated samples

$$n = mD \quad (1.25)$$

The resulting output is

$$y[m] = \sum_{k=0}^{\infty} h[k]x[mD - k]. \quad (1.26)$$

One of the most commonly used applications of decimation is known as oversampling. Referring back to (1.14), it was shown that quantization noise power was a constant quan-

tity. This power, assuming a band limited signal, is evenly distributed over a frequency range of $0 \leq P_n \leq F_s/2$. Based on this observation, the noise floor could be lowered by sampling at a rate higher than that required by the Nyquist Theorem thus using a fraction of the available bandwidth. Decimation is then used to lower the effective sampling rate thus reducing both noise and lessening hardware requirements. An illustration of this concept is presented in Figure 1.19. The oversampling ratio is defined by

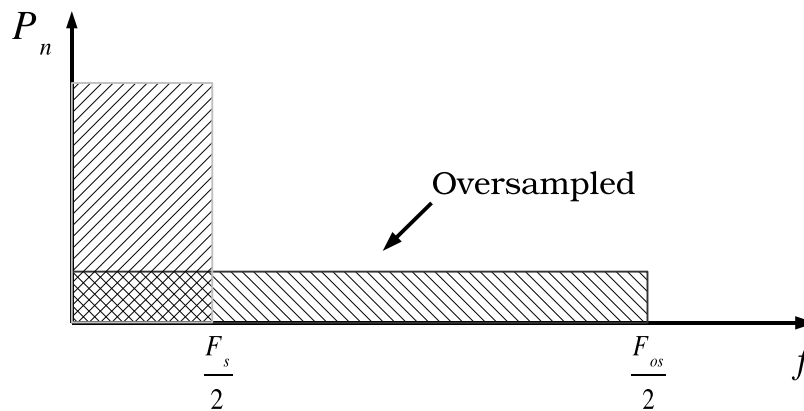


Figure 1.19: Quantization noise power

$$OSR = 10 \log \left(\frac{F_{os}}{2B} \right) \quad (1.27)$$

where F_{os} is the oversampled rate and B is the bandwidth of the sampled signal. Including the OSR to (1.16)

$$SQNR = 10.79 + 6.02b + 10 \log(FFS) + OSR. \quad (1.28)$$

Interpolation, or up-sampling of a signal by an integer I is accomplished by inserting

$I - 1$ zeros between each sample of the signal. If the original sample rate is F_s , the interpolated rate becomes

$$F_I = IF_s. \quad (1.29)$$

Using $v[m]$ to represent the interpolated sequence, the result becomes

$$v[m] = \begin{cases} x\left[\frac{m}{I}\right] & m = 0, + - I, + - 2I, \dots \\ 0 & otherwise \end{cases} \quad (1.30)$$

Interpolation, as shown equation (1.30), effectively increases the bandwidth by a factor of I . As a result, $v[m]$ must be filtered by

$$H_I[\omega] = \begin{cases} 1 & -\frac{\pi}{I} \leq \omega \leq \frac{\pi}{I} \\ 0 & otherwise \end{cases} \quad (1.31)$$

This filter is used to remove duplicate images from the original sampled sequence. This concept is illustrated graphically in Figure 1.22. A block diagram of this operation

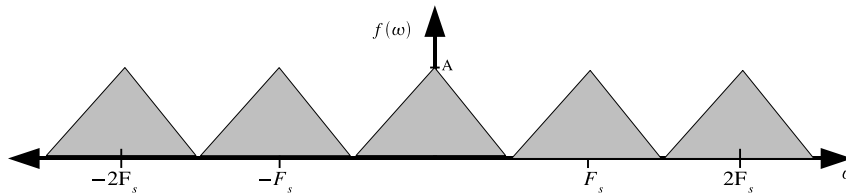


Figure 1.20: Sampled images

is shown in Figure 1.23. In many applications, a non-integer rate change is needed to meet system requirements. An example of this is the conversion of an audio CD format into a standard DAT format. This operation requires a rate change from the CD rate

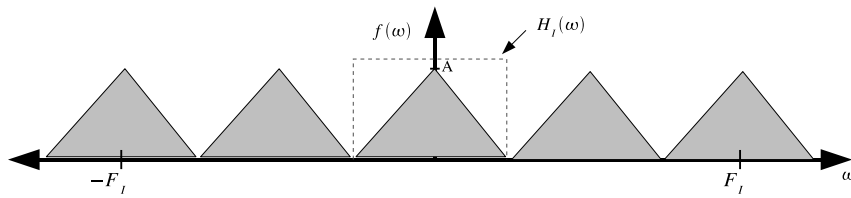


Figure 1.21: Interpolation Image Filter

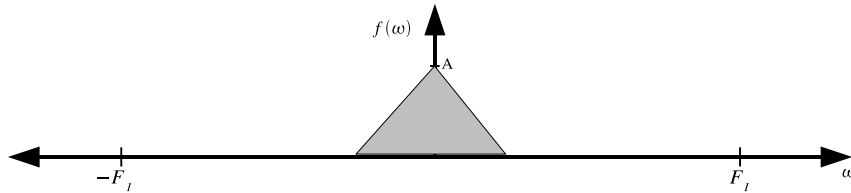


Figure 1.22: Resulting spectrum after interpolation

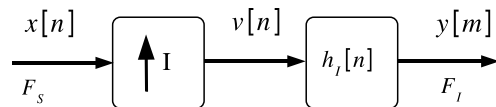


Figure 1.23: Interpolation Block Diagram

of 44.1kHz to the 48kHz rate of the DAT format. This can be accomplished through a combination of interpolation and decimation. First the signal is interpolated by a factor I , filtered, and then decimated by an integer factor D .

$$F_R = F_s \frac{I}{D}. \quad (1.32)$$

In this case the filter will remove frequencies above the final Nyquist rate thus supplying the function required by both interpolation and decimation. This operation allows for any combination, within hardware limits, of rational rate changes and commonly referred to

as a *resampler*. Using a combination of interpolation and decimation, a number of filter techniques have been created to optimize performance in a DSP system. Application of these filters will be discussed in chapter 2.

1.4 Software Analysis and Design

As the electronics industry and the resulting products advance in complexity, software development is beginning to play a primary role in overall product design. The boundary between electrical engineers and software engineers is diminishing rapidly [12]. In this section an overview of object oriented programming (OOP) will be given along with a review of relevant material from the Unified Modeling Language (UML). Together, these tools provide a method for understanding and alleviating complexity in software design as well as provide more robust software.

1.4.1 Object Oriented Programming

OOP was created out of a need to efficiently develop systems that were rapidly increasing in both size and complexity. This section will provide a brief overview of the role OOP plays in modern software design.

It is a known fact [11] that humans, in general, are only able to manage a maximum of seven items simultaneously without error. Even small, well-understood systems can present difficulties to the human mind. As a result, humans tend to reduce complexity by partitioning a system into smaller, manageable pieces. In the case of top-down design, systems are partitioned by function; this is also known as procedural programming and has been the most widely used method of design since the advent of modern computers. As system complexity increases, the top-down design methodology begins to expose

weakness in many areas such as: 1) readability, 2) maintainability, 3) adaptability, and 4) expandability. The biggest problem with procedural programming, as seen by language developers, is that responsibility is confined to one primary thread of control (main loop). All of this responsibility in one place complicates coding and typically requires extensive changes to accommodate small variations in design. Additionally, readability is reduced thus making software maintenance more costly and time consuming. As an alternative, researchers, in the 1970s, began to explore the idea of partitioning a system through objects; and, by 1986, a number of object oriented languages were available. As seen from the object oriented (OO) perspective, a system is composed of a collection of objects, each with a well-defined behavior, that interact and collectively define the system. Partitioning a system through object decomposition results in many important characteristics. Object re-use is made possible through inheritance, which is the ability for an object to assume another object's characteristics while reserving the ability to modify/add more as needed. Encapsulation, the ability to hide complexity from the user, is possible by exposing the object's interface while hiding the inner complexity. In addition, the system becomes easily adaptable/expandable since changes are made to the required object. The ability to understand and maintain the system is lessened due to well-defined boundaries between objects. Of the many languages available for OOP, C++, due to widespread use and support for graphical user interfaces (GUI), was chosen for this project. Interested readers are referred to [4, 19] for complete coverage of OO analysis and design.

1.4.2 Unified Modeling Language

The UML is a graphical modeling system created to aid in the design of complex Object Oriented based software systems. One of the most important uses of this modeling

language is its ability to bridge the gap between the software user and the software developer. Strong communication between the system user and the developer is the most important concept determining the success or failure of a design. The UML fills this gap by abstracting system complexity into a set of interfaces and interactions, which can be reasonably understood with minimal effort. This benefits not only the user of a complex software system but also aids in the design of such systems by reducing complex object interactions into a visual representation. The UML was released to the public in 1997 by the Object Management Group (OMG) and has seen many revisions over time. Use of the UML, as it relates to this thesis, is limited to a small subset of diagrams that were found most suitable for this design. The following diagrams will be used:

1. Use Case: Illustrate interactions between the system's users and the system itself. This is used at the beginning of a design to gather all user interactions with the system; and, consequently build a list of system requirements.
2. Class Diagram: Used to illustrate interactions between a collection of objects in the system. They are also used to provide a list of properties and methods available to each class.
3. Activity Diagram: Provide insight into the operation of a subset of the system or an overview of the entire system. These diagrams resemble flow charts used in procedural modeling but provide methods for illustrating concurrent activity commonly seen in OO systems.
4. Composite Structure: Depict a broad view of a class by displaying the class interface along with a description of components functioning inside the class. This is accomplished by displaying the class's internal functions using smaller blocks.

Chapter 2

System Analysis and Design

Implementation of any design begins with a complete definition of the problem followed by a method of action to achieve the desired solution. This design used an object oriented methodology and was chosen based on the ability of OO design to efficiently manage complexity and make the system resilient to change. Within the OO paradigm, an overwhelming number of techniques and approaches exist and more than one were implemented in this design. This section will discuss aspects of the system from a design perspective. Both hardware and software discussions are combined to better communicate their dependence. To begin, a precise definition of the problem domain, with the help of domain experts, is the first stage of design known as *requirements analysis*[6]. The sections that follow will discuss the techniques used to analyze, model, and implement the design. Detailed discussion of both hardware and software are combined to better communicate their interdependence.

2.1 Requirements Analysis

Definition of the system's capabilities and features are best defined by users (domain experts) of the system. A preliminary list of requirements were created as a first step in the design process:

1. Users are typically visiting scientists and will receive limited assistance from staff.
2. Users need the ability to configure the system to meet their own specifications.
3. System configuration should be stored for later re-use.
4. Multiple configurations, cycled at predetermined intervals, are sometimes necessary for a single experiment.
5. The system will use the Linux Operating System.
6. Some experiments require large bandwidths and high storage rates.
7. Minimal real-time processing and plotting tools are necessary to ensure proper setup and equipment function.
8. Telescope position and sytem time are broadcast (multicast) on the network and must be processed and stored.
9. A standard file format will be required for data storage and retrieval.
10. Software should be able to accommodate newer hardware revisions with minimal effort.
11. Documentation must be written to assist both developers and users.

The list served as a framework for the design and each item was organized by function. Primary operations were identified and further refinement produced smaller, well-defined supporting. A Use Case Diagram, shown in Figure 2.1, depicts the system visually; displaying system functionality and roles of the different users. From the analysis, 4 pri-

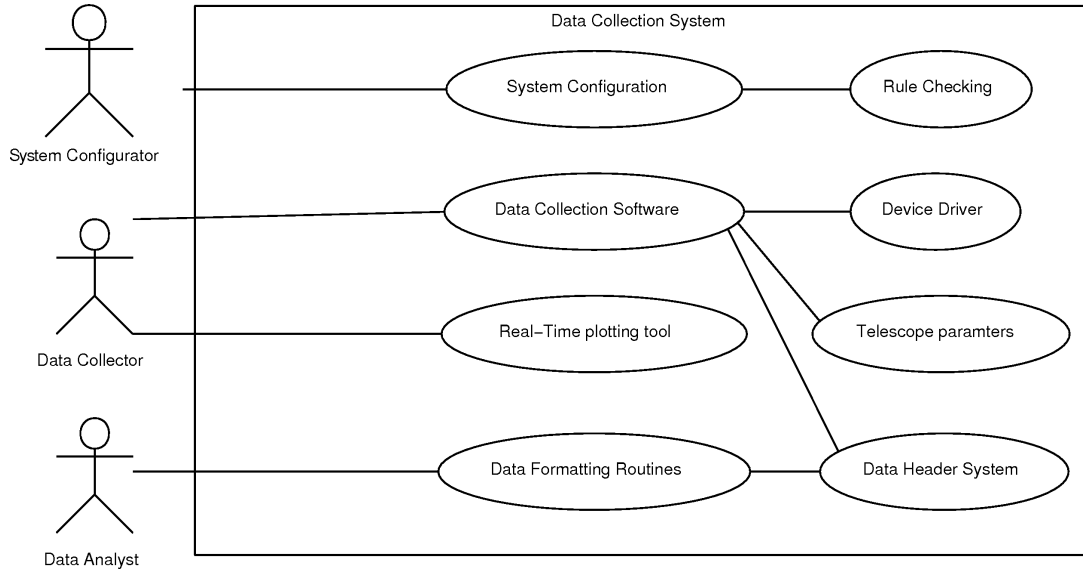


Figure 2.1: Use Case Analysis

mary and 4 supporting operations were discovered; and, having well-defined boundaries, partitioned the system into 4 primary programs of operation:

1. System Configuration Program
2. Data Collection Program
3. Real-Time plotting Program
4. Data Formatting Routines

These 4 programs fully define the system's operation from a software perspective. In this design, engineers at AO had previously selected all hardware; therefore, integration of

software with existing hardware became the focus. A list of all interacting hardware is given as follows:

1. Digital Receiver,
2. General Purpose Computer,
3. High speed, large capacity data storage, and
4. Radar pulse controller.

Digital Receiver

The Echotek-GC214-PCI (GC214) Digital Receiver was chosen for the system because of its ability to provide many modes of operation; accommodating a large variety of possible experiments at the observatory. The GC214 consists of 2 analog inputs, each sampled by an AD6645 14-bit ADC. A simplified diagram of the GC214 is depicted in Figure 2.2. In the sections that follow, the GC214's capabilities and functionality are

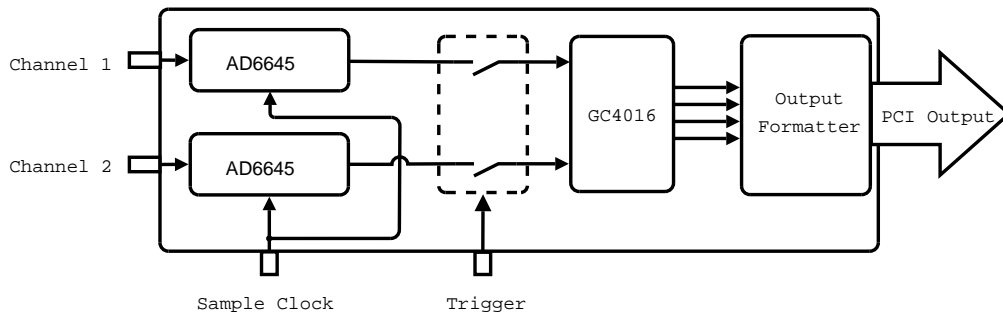


Figure 2.2: Echotek-GC214PCI Diagram

described in detail, with each section introducing a component of hardware followed by its accompanying software. The intention of this approach is to maintain coherence between software and hardware.

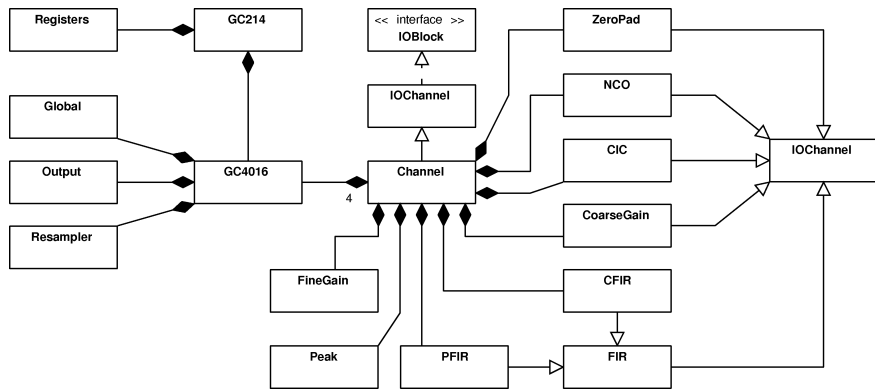


Figure 2.3: GC214 Class Diagram

2.2 System Configuration

The GC214 digital receiver is a versatile device, capable of multiple modes of operation. Taking full advantage of these capabilities requires a full featured software interface; providing complete control over parameters while maintaining simplicity. Encapsulation [4] is a commonly used technique to hide complexity; exposing only the necessary features of a system to its user. In this design, a graphical user interface (GUI) was used to provide a clean, simple interface; again, exposing only parameters necessary and familiar to the user while hiding the bulk of complexity. Configuration software for the GC214 is responsible for the following tasks:

1. Provide a simple, easy-to-use graphical interface with commonly used layout techniques.
2. Provide rule checking to alert the user and prevent improper settings.
3. Record the user's minimal requirements and compute all remaining variables required to configure the hardware.

Additionally, a key component of this design was to produce a system resilient to change; meaning that hardware upgrades would require minimal alterations to software. A number of components are needed to successfully perform all tasks required of a Digital Receiver. A break-down of the GC214 is shown in Figure 2.3 and displays components directly involved with system configuration. The GC4016 Digital Down Converter integrated circuit (IC) [21] is the primary component on the GC214. The GC4016 is an Application Specific Integrated Circuit (ASIC) used to perform all data processing. The GC4016 consists of 4 independent processing channels that perform signal down-conversion, filtering, and data rate adjustments. Each of the 4 channels can operate independently or can be combined to increase channel band-width. The GC4016, by design, contains modules with well defined boundaries making it suitable for object decomposition. Each of the modules, as stated in the manual [21], were used as objects in software:

1. Input Format
2. ZeroPadding
3. Numerically Controlled Oscillator (NCO)
4. Cascaded Integrated Comb Filter (CIC)
5. Coarse Gain
6. 21 Tap Finite Impulse Response Filter I (CFIR)
7. 63 Tap Finite Impulse Response Filter II (PFIR)
8. Fine Gain

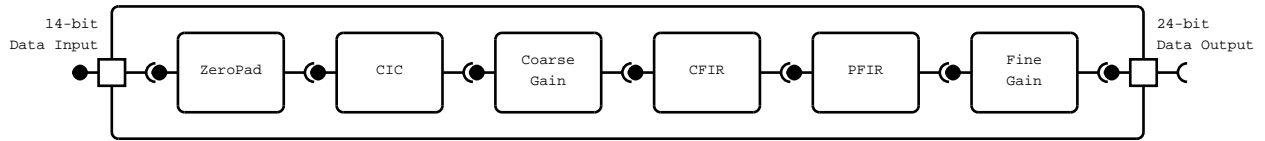


Figure 2.4: GC4016 Channel

9. Resampler

In the GC4016 datasheet [21], both Input Format and Resampler modules are members of the channel. Further analysis revealed that the modules responsibilities were common to all channels, therefore these modules were separated from the channel. This separation produced classes that were more cohesive and loosely coupled. The Channel diagram in Figure 2.4 illustrates this concept. Analysis of commonalities and variances [] among the channel’s modules revealed a key abstraction. Each module has the following common attributes: 1) Input rate, 2) Output rate, 3) Input gain, and 4) Output gain. These common traits were used to create an interface class named *IOBlock* as shown in Figure 2.5. In addition, each module within the channel is a part of a larger, cascaded

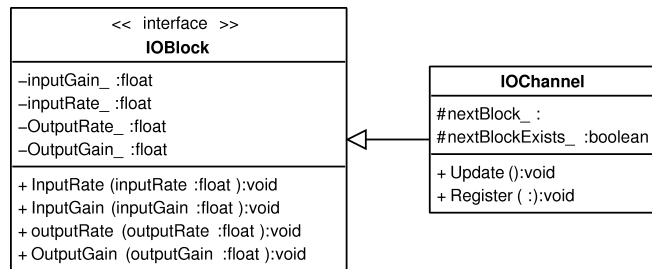


Figure 2.5: *IOBlock* Interface and *IOChannel* Class Diagrams

system. This type of system is characterized by a succession of stages where the output of each stage provides the input for the next. This relationship shows a dependence among interconnected modules. A change to one module’s parameters requires an update of all

modules that follow. This behavior was implemented by creating an abstract class named *IOChannel* which inherits the *IOBlock* interface. Two methods were created to emulate the cascading system as shown in Figure 2.5. Each object must register the next object in the system via a base class pointer. Changes to a module invoke its *Update* member which in turn calls its registered object's *Update* member. Each subsequent module is synchronized in this manner. Preceding stages are unaffected by this operation. Declaring the *Update* member virtual allows derived classes to implement custom behavior. Each module in the GC4016 channel inherits the *IOChannel* class.

ZeroPad Module

The first stage in the GC4016's channel is the zero pad function. Zero padding is a technique used to match the input data rate and the sample clock rate when the data rate operates at a lower rate. Zeros are inserted between each input sample. From the sample clock's perspective, the input data rate is increased. Due to the apparent rate increase, the user is able to choose a lower input rate. To ensure proper operation, the input rate must meet specifications given by

$$InputRate = \frac{f_{clk}}{nzero + 1}, \quad (2.1)$$

where *nzero* is the number of zeros to insert. Valid values are integers ranging from 0 to 15. Input rates as low as $f_{clk}/16$ are possible. Time Domain Multiplexing (TDM) is another application requiring zero padding. In this application multiple channels of data are serialized into a single data stream, separated by time. In this system, *nzero* is set to the number of data channels. The zero pad function uses programmable synchronization and, in the case of TDM, is required to sample the desired data channel. The zero pad

function uses a programmable sync input to synchronize sampling in this stage. The output gain of the zero pad function is represented by

$$Gain = \frac{1}{nzero + 1}. \quad (2.2)$$

Software implementation for the zero pad function began with a description of the hardware interface as illustrated in Figure (2.6). As the first stage in the system, input gain is constant. The zero pad function has no control over the data rate. This is illustrated with a straight bar connection from input rate to output rate. The *ZeroPadding* method sets the number of zeros inserted into the data stream. The *ZeroPadSync* method selects the proper source for synchronizing collected samples.

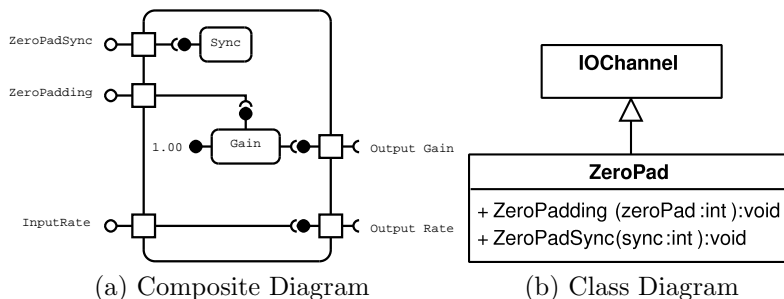


Figure 2.6: ZeroPad Diagrams

CIC Module

The Cascade Integrator Comb filter [7, 8] is an efficient implementation of cascaded FIR filters combined with, depending on the design, either decimation or interpolation. The CIC is commonly used in multirate systems where large rate changes are desired. The CIC has the following benefits over the standard FIR filter:

1. No multiplications are required.

2. No storage required for filter coefficients.

The FIR transfer function has the form

$$H(z) = \sum_{k=0}^{K-1} h[k]z^{-k} \quad (2.3)$$

where h is the impulse response kernel, k is the delay, and K is the number of coefficients. Noting that (2.3) is a finite geometric series, the basic structure of a single stage CIC is realized from the latter part of (2.4).

$$S_K = \sum_{k=0}^{K-1} ar^k \equiv \frac{a(1-r^K)}{1-r} \quad (2.4)$$

Setting coefficients to unity and letting $r = z^{-1}$, the CIC transfer function becomes

$$H(z) = \left[\frac{(1-z^{-RM})}{1-z^{-1}} \right]^N \quad (2.5)$$

where R is the decimation factor, M is differential delay, and N is the number of cascaded stages. The CIC implementation uses a combination of integrators and comb stages, combined with a rate changing mechanism such as interpolation or decimation. A single stage integrator is used to represent the pole of the transfer function in (2.5). The realization of this stage is illustrated in Figure 2.6 and the is described by

$$y[n] = x[n] + y[n-1]. \quad (2.6)$$

The transfer function is

$$H_I(z) = \frac{1}{1-z^{-1}}. \quad (2.7)$$

A multi-delay comb filter is used to represent the zeros of the transfer function in 2.5.

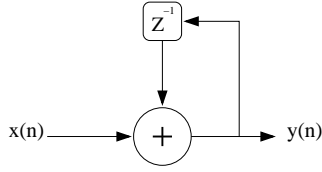


Figure 2.7: Single Stage Discrete Integrator

Figure 2.8 illustrates the characteristics of the filter. The comb filter's response is

$$y[n] = x[n] - x[n - N] \quad \text{where } N = \text{differential delay} \quad (2.8)$$

The transfer function is described by

$$H_C(z) = 1 - z^{-N} \quad (2.9)$$

Multirate systems generally require large rate changes which increase coefficient storage

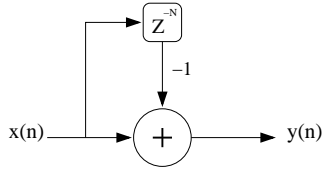


Figure 2.8: Single Stage Discrete Differentiator

in the comb stages. Coefficient storage can become excessive when cascading multiple stages. This large delay is eliminated by using decimation/interpolation. The CIC limits the comb filter's delay to 1 or 2, which is known as the differential delay (M). All other delay is introduced through standard multirate techniques. An illustration of the GC214's Decimation CIC filter is seen in Figure 2.9 CIC gain is determined by

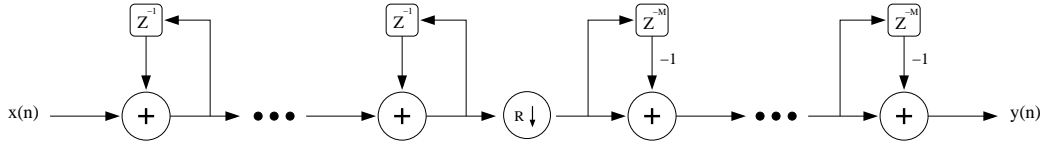


Figure 2.9: MultiStage Decimating CIC Filter

$$\text{Gain} = RM^N. \quad (2.10)$$

The GC214 uses a unity differential gain resulting in removal of M from 2.10. Gain compensation is necessary to prevent data overflow. The GC214's gain compensation equation is

$$\text{Comp} = 2^{\text{Shift} + \text{Scale} + 6\text{BigScale} - 62} \quad (2.11)$$

where variable ranges are:

1. $0 \leq \text{*Shift} \leq 7$
2. $0 \leq \text{Scale} \leq 5$
3. $0 \leq \text{BigScale} \leq 7$

* range from 4-7 when using 20 bit rounding. The overall gain equation of the CIC is

$$\text{CIC Gain} = R^N 2^{\text{Shift} + \text{Scale} + 6\text{BigScale} - 62} \quad (2.12)$$

Rewriting (2.12) and accounting for ZeroPad gain, proper gain compensation can be realized by

$$\text{Shift} + \text{Scale} + \text{BigScale} \leq 62 - N \log_2(R) + \log_2(\text{nzero} + 1). \quad (2.13)$$

Violation of this rule will result in undetected data overflow and an automated algorithm was implemented to prevent this occurrence. The CIC module is derived from IOChannel and is responsible for the gain, decimation, and multichannel options that will be discussed in a later section. The CIC module class diagram is illustrated in Figure 2.10. The CIC module interface is shown in Figure 2.10. Gain synchronization is provided via

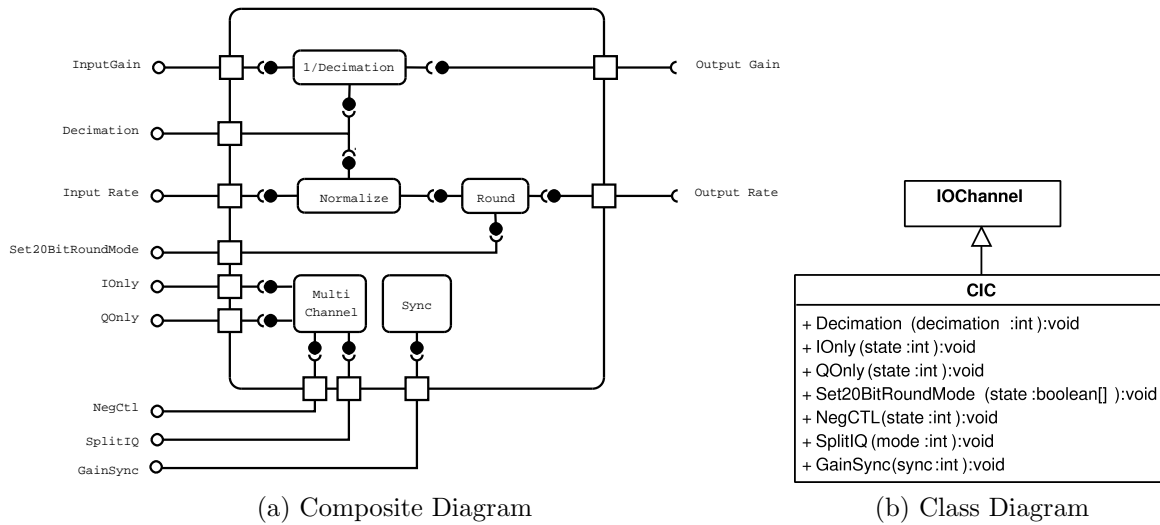


Figure 2.10: CIC Diagrams

the *GainSync* member. Output data can be rounded to 16 or 20 bits, with decimation greater than 3104 limited to 16-bit rounding. A gain normalization algorithm is provided to optimize variables for unity gain, and prevent data clipping due to improper settings. The CIC's *Normalize* member optimizes: 1) shift, 2) scale, 3) and bigScale variables. The code segment in 2.1 illustrates the algorithm.

```

void CIC::Normalize(){
    shift = 7; bigScale = 0; scale = 5;

    float rightValue = 62.0f - (5.0f*log(static_cast<float>(decimation)) +
        log(InputGain())) / log(2.0f);

    float leftValue = scale + shift + 6.0f*bigScale;

```

```

while((leftValue < rightValue) && (bigScale != 7.0f)){
    ++bigScale; leftValue += 6.0f;
}

while((leftValue > rightValue) && (shift != 4.0f)){
    --shift; --leftValue;
}

while((leftValue > rightValue) && (scale != 0.0f)){
    --scale; --leftValue;
}

while((leftValue > rightValue) && (shift != 0.0f) && !mix20b){
    --shift; --leftValue;
}
}

```

Listing 2.1: CIC Normalize Algorithm

Coarse Gain Module

Although the CIC filter produces an efficient decimating filter, its gain as a function of frequency is undesirable and requires compensation. The *Coarse Gain* module is used to boost gain up to 42 dB in 6 dB steps. The CIC filter’s overall gain is dependent on the value of decimation chosen. As discussed in the previous section, the CIC filter’s gain must be unity or less in order to prevent the clipping of data. The *Coarse Gain* class, being a member of the GC4016’s processing chain, inherits the *IOChannel* interface. Both interface and class diagram are illustrated in 2.14. The *AutoGain* method was added for automatic gain compensation and is optimized for unity gain. Input data width is 20 bits and output data is rounded to 24 bits. The input rate is unaffected.

FIR module

Multirate filtering techniques reduce computation costs by implementing multiple cascading filters to produce the desired response. Individually, a single stage can not provide the

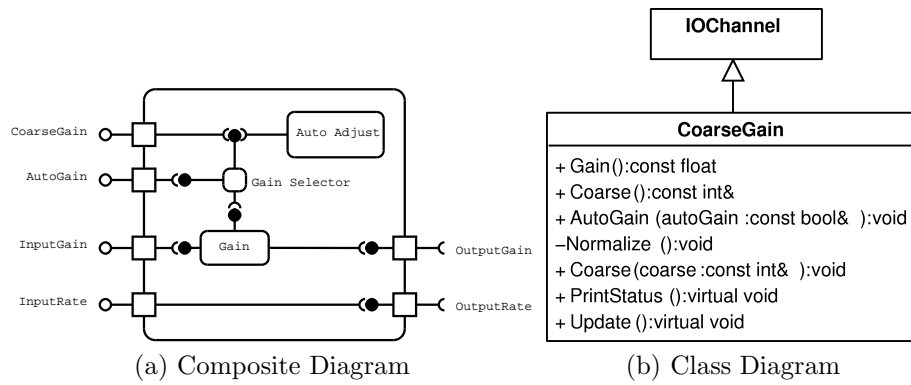


Figure 2.11: Coarse Gain Diagrams

desired response due to the limited number of coefficients used to represent the transfer function. Instead, each stage provides a relaxed transition band and followed by decimation which effectively lowers the filter’s data rate, thus providing an a good response without a large number of filter coefficients. A typical FIR response is

$$H[n] = \sum_{k=0}^N h[n]x[n - k] \tag{2.14}$$

where n is the sample number, k is the delay, and N is the length of the filter.

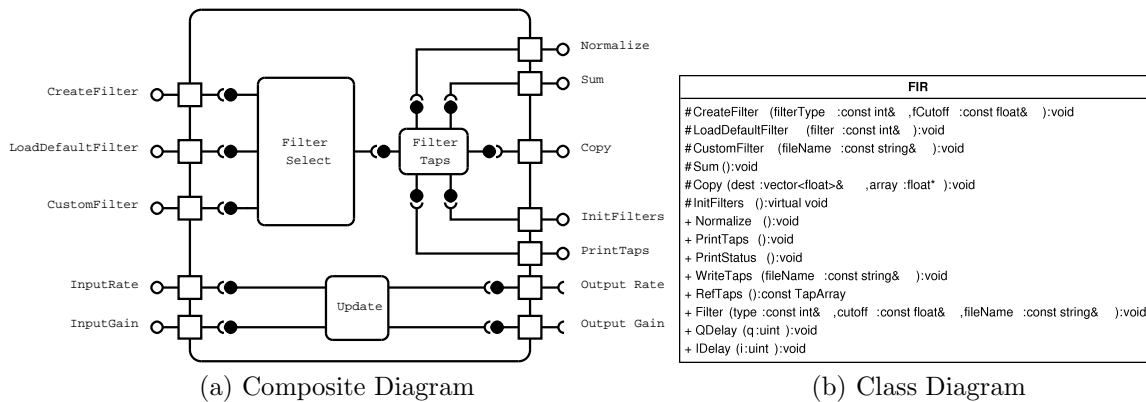
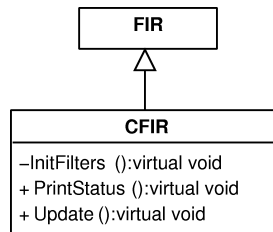


Figure 2.12: FIR Diagrams

CFIR Module

The CFIR module is 31 coefficient decimate by 2 FIR filter. The CFIR filter is typically used to provide droop compensation for the CIC's imperfect passband response. It can also be used to complement the PFIR's response if needed. An illustration of the filter is shown in Figure ().

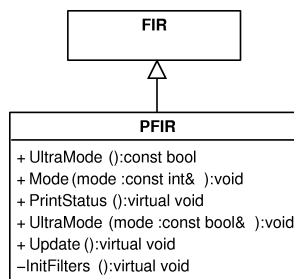


(a) Class Diagram

Figure 2.13: CFIR Diagrams

PFIR Module

The PFIR module is a 63 coefficient filter that decimates by 2 in both Narrowband and Wideband modes. UltraWideband mode cancels decimation in this filter by applying a single sample phase delay between even and odd samples in the processing channels. This filter is typically used to provide a customized response.



(a) Class Diagram

Figure 2.14: PFIR Diagrams

Fine Gain Module

The fine gain module is capable of precise gain adjustments using a programmable variable *Fine* in

$$G_f = \frac{Fine}{1024}, \quad (2.15)$$

where *Fine* is a 14-bit integer; providing a maximum gain of $24dB$. Figure 2.15 depicts the *FineGain* module. The purpose of the *FineGain* module in this system is to fine-tune

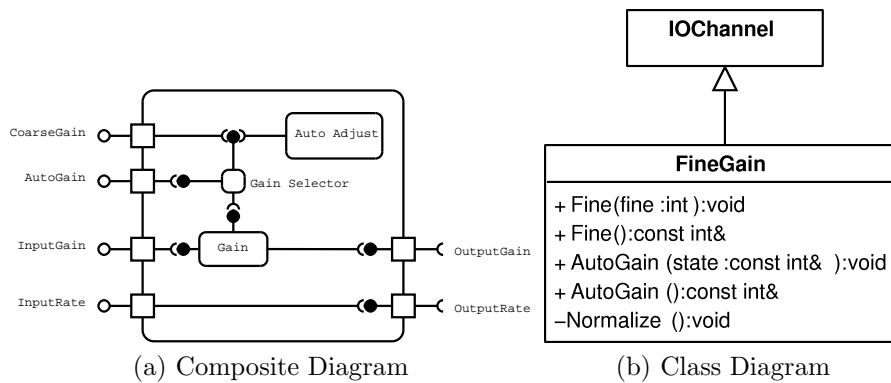


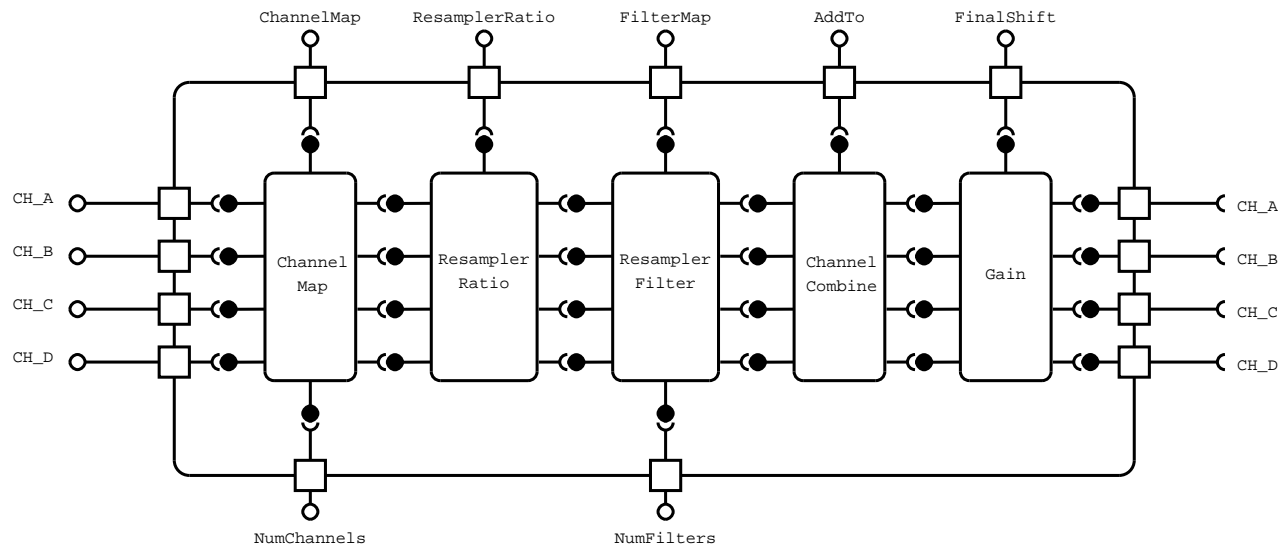
Figure 2.15: Fine Gain Diagrams

the gain with the goal of achieving unity gain in the system.

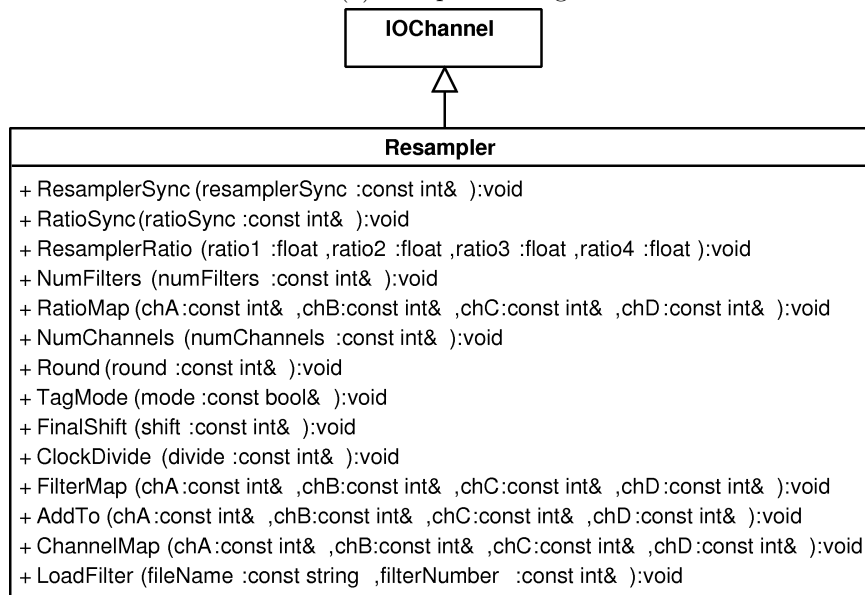
Resampler Module

Resampling is a process of increasing or decreasing the system's sample rate to meet sampling requirements of the interfacing system. In this system, the interfacing hardware is the GPC and the hardware is capable of rates beyond the GC214; therefore, no specific need for resampling exists. In order to maintain resilience and allow other observatories to use this software, a complete resampler module was created. In addition to resampling, the resampler module also provides an additional 512 coefficient FIR filter that can be partitioned in a variety of ways or used as a single filter. Gain is also provided in the

resampler module but should only be used to make coarse adjustments. Figure 2.16 illustrates the Resampler Composite and Class diagrams.



(a) Composite Diagram



(b) Class Diagram

Figure 2.16: Resampler Diagrams

2.2.1 Configuration Graphical Interface

All interaction with system configuration takes place through a custom designed GUI using Trolltech's QT libraries [1]. Basic variables are entered through the system's main window shown in Figure 2.17. Automated rule checking is provided and corrections

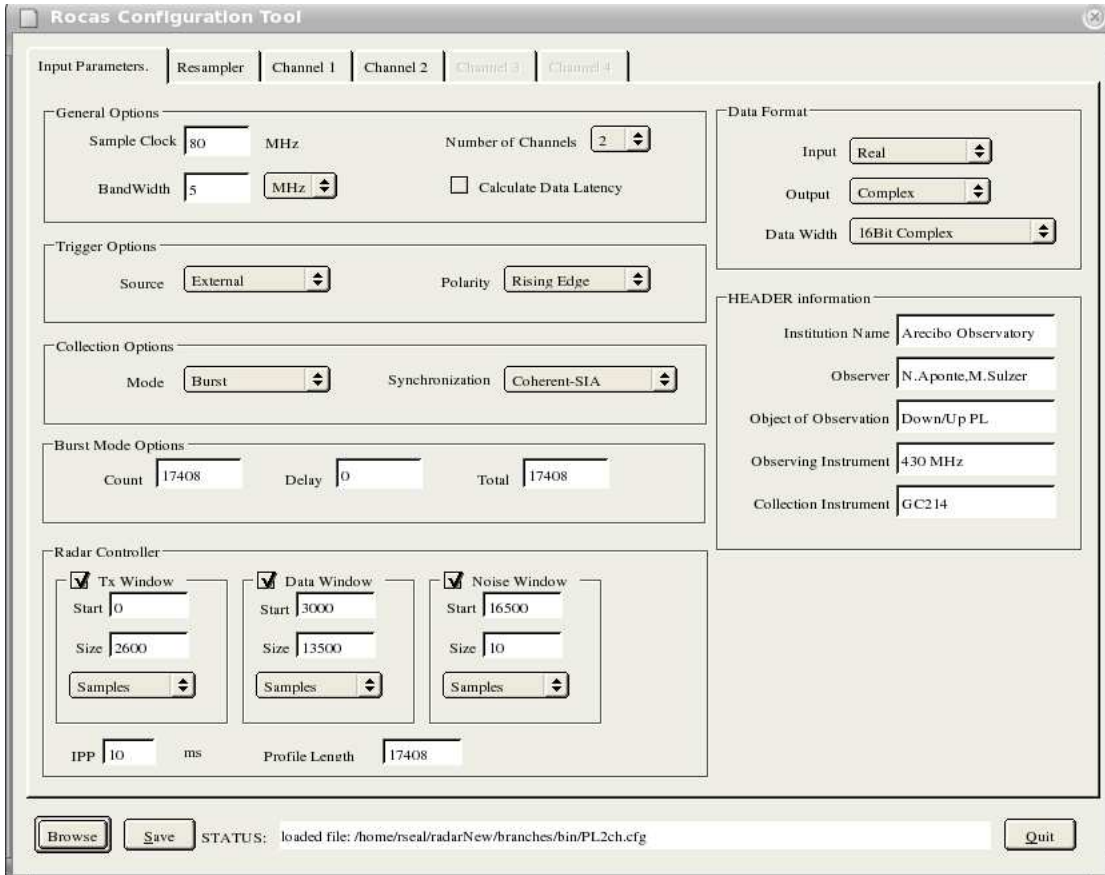


Figure 2.17: Main Configuration Window

are made when the user chooses and incorrect or invalid setting. A status window is provided to display necessary information as the configuration is taking place. Based on the bandwidth and the number of channels required, additional windows are available for programming. These additional windows allow the user to configure each channel individually to meet requirements; this includes the channel's output rate, gain, and

filtering as illustrated in Figure 2.18.

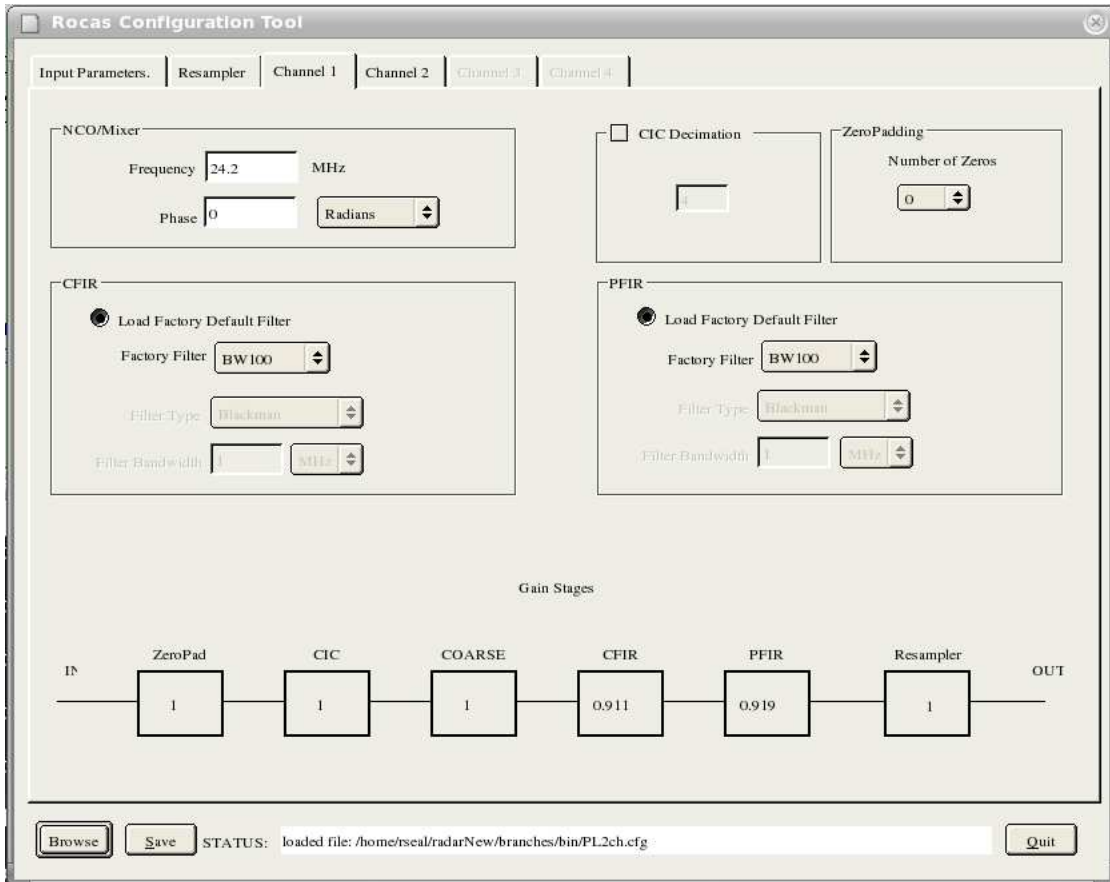


Figure 2.18: Channel Configuration Window

When the user has completed configuration, three files are saved to disk: 1) ASCII based configuration file 2) file containing binary data for card and device driver configuration 3) Primary header data used in data acquisition data formatting The configuration file is used by the configuration program to reload/restore a previous configuration. The other two files are used by other programs in the system.

2.3 Data Acquisition

2.3.1 Hardware / Software Interface

Design and implementation of modern DAS present many inherent challenges; of these, the largest lies in the ability to efficiently handle the high rate of data into the system. PC peripherals provide a variety of paths for data transfer. Currently, the PCI bus and its derivatives offer the highest performance; consequently, the Echotek-GC214 digital receiver uses a 32-bit PCI bus with a clock rate of 33MHz. This standard provides up to 133 MB/s continuous transfer rates with the OS overhead reducing actual rates to approximately 75% of this maximum ???. The host side (PC) of the system, the device driver is responsible for all transactions; including data transfers. A custom device driver was created to maximize data transfer to the PC. This was achieved using Direct Memory Access (DMA) transfers. More specifically, chaining DMA transfers were implemented via a DMA descriptor table. DMA operates by directly transferring data from hardware to memory with limited intervention from the processor. In some applications, even larger blocks can be transferred by applying DMA descriptor tables. The Echotek-GC214 uses the PLX9080 PCI interface integrated circuit for communication. The PLX9080 descriptor table is illustrated in Figure 2.19. Large numbers of descriptors can be used and are connected by the descriptor's next pointer. In this implementation, each table contains 1 second of data, with a data block size of 4 kB. The chosen block size allows alignment with the OS page size, which is also 4 kB. Alignment on page boundaries provides many benefits that will be discussed shortly. At the end of each table of descriptors, a special bit is set in the descriptor's control register; triggering an interrupt to alert the user of incoming data. In addition, 4 small FIFOs, one for each channel, are located on the digital receiver; providing minimal time for DMA to operate. Timing requirements for

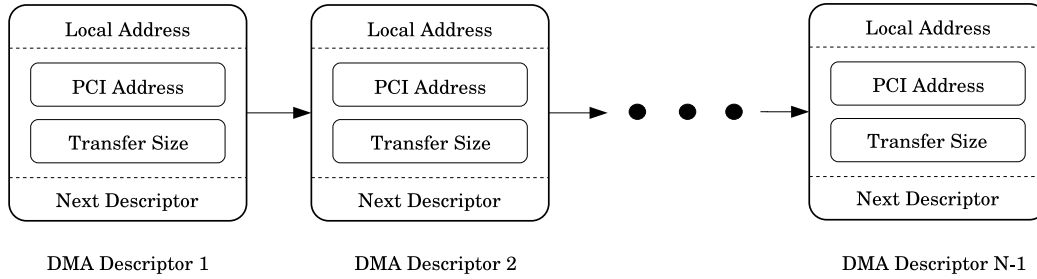


Figure 2.19: PLX9080 DMA Descriptor Layout

such systems are depicted in figure 2.20. Each of the FIFOs depicted in Figure 2.20

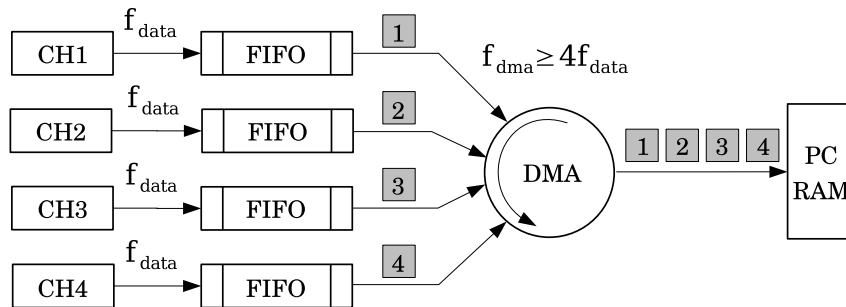


Figure 2.20: Echotek-GC214 FIFO Layout

are 64x32 kB in length, with each channel capable of transfer rates up to 9.54 MSPS. To prevent data loss, maximum sustainable rates of 38.15 MSPS must be achieved. In addition to data transfer, many other tasks are needed for full operation: 1) Partial selection data for storage. 2) System verification using real-time data displays. 3) Header information is to stored data. To fulfill the complete requirements of the system, a combination of techniques were employed: 1) dual-layer buffer system utilizing both kernel

and user levels of the OS 2) the producer/consumer threading model 3) shared memory via the *tmpfs* filesystem Dual-layer buffers are widely used in audio application software and provide multiple buffers to mask system delays which would normally produce unacceptable sound performance. In this particular system, a lower level set of buffers, called DMA buffers, are allocated by the device driver; making these buffers kernel allocated buffers. In many Operating Systems, two levels of priority are used when dealing with interactions:

1. Kernel mode - this level is reserved for low level system management required by the operating system. Device drivers are run in this mode; preventing the common user from potentially damaging devices through direct hardware control.
2. User mode - this is the mode used by system users and application programmers. The user interacts, as needed, with kernel mode through the use of well defined system calls provided by the operating system.

The Echotek-GC214 device driver manages the kernel allocated DMA buffers and offers user access using the *mmap* system call. The *mmap* function, known as memory mapping, allows the user to map kernel allocated memory into user space using standard C language file I/O functions. In order to minimize memory management at the kernel level, provide real-time plotting capabilities, and provide flexibility to the user's application software, a secondary buffer system was allocated in user space. Additionally, this system utilizes the Linux OS's shared memory capabilities. Shared memory, as the name implies, allows a user's process (running program) to include the shared memory's address space in its own space; consequently, the user's process can treat the memory as its own. A specialized filesystem [16] called the *tmpfs* filesystem was used to provide a clean interface to shared memory. This filesystem allows the user to create files in PC RAM using standard

function calls. Memory management is handled through a simple file I/O interface. Figure 2.21 depicts memory use and layout. Efficient operation and synchronization is

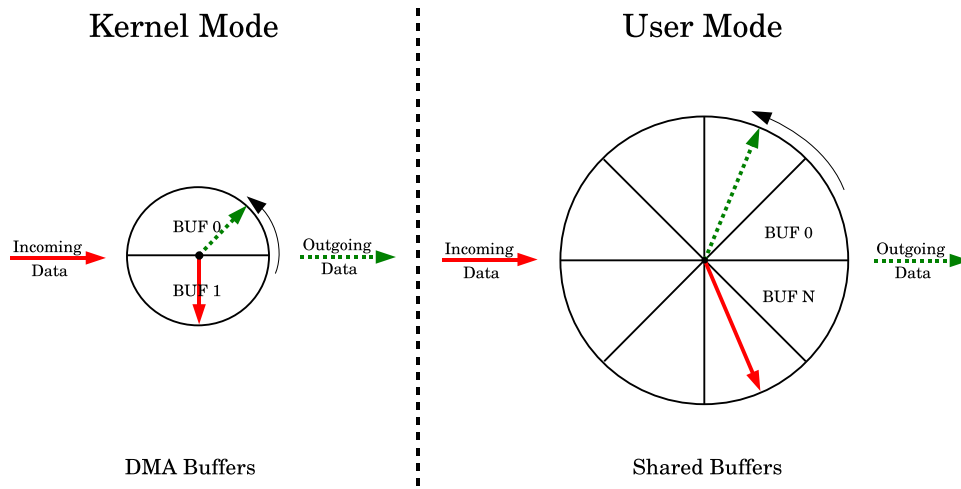


Figure 2.21: Memory Buffer Layout

accomplished with the producer/consumer (P/C) threading model [3]. The P/C model requires two threads: the producer thread handles data writes to the buffers, and the consumer thread manages data reads as shown in Figure ?? . Synchronization is controlled through a shared variable that tracks dirty buffers (buffers containing pending data). In this model, the consumer thread starts the sequence, requesting data from the first buffer. If data is not available, the consumer thread is put to sleep. Then, the producer begins filling buffers at a continuous rate; waking the consumer thread upon completion of a buffer. This operation continues indefinitely using a predetermined number of buffers. Non-real-time operating systems can impose unpredictable latencies [2]; violating real-time operation. Applying the P/C model, latencies can be masked through buffering; bypassing the need for a real-time operating system. Additionally, use of this model, combined with shared memory regions, allow for multiple levels of real-time processing

to occur simultaneously. This approach preserves storage device bandwidth which is critical for high speed, real-time data writing. This provides a major advantage over older systems in which the storage device spent a large amount time seeking to satisfy system reads and writes; further limiting bandwidth. Radar data collection begins

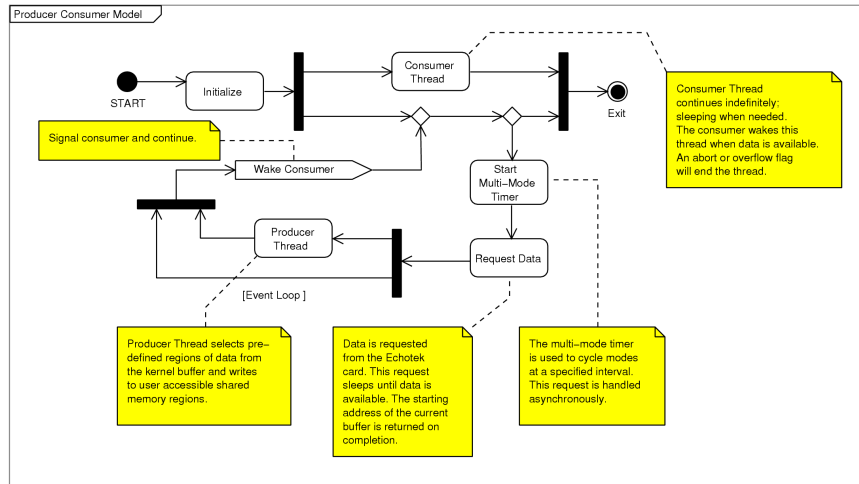


Figure 2.22: Producer Consumer Activity Diagram

when a trigger signal is applied to the external gate of the digital receiver. Next, the user application requests data from the digital receiver, via the driver's interface. When data is available, the user application selects a segment of data and copies it into a secondary, user allocated buffer system. This secondary system allows data sharing among multiple processes by utilizing the *POSIX shared memory library* and the *tmpfs* [16] file system. *Tmpfs* transparently allows large regions of PC RAM to be used as a standard storage device. This filesystem is, by default, dynamically sizable through the use of swap space. For high speed operation, a fixed size *tmpfs* is required; preventing interaction with swap space which drastically degrades performance. The *POSIX shared memory library* uses the *tmpfs* filesystem to allocate regions of memory included in the requesting process's own address space; providing data sharing among processes. All experiments

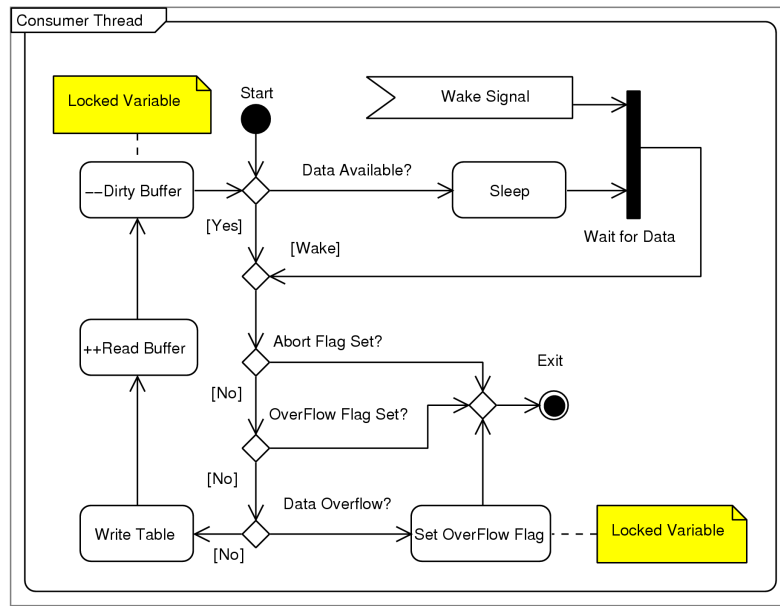


Figure 2.23: Consumer Activity Diagram

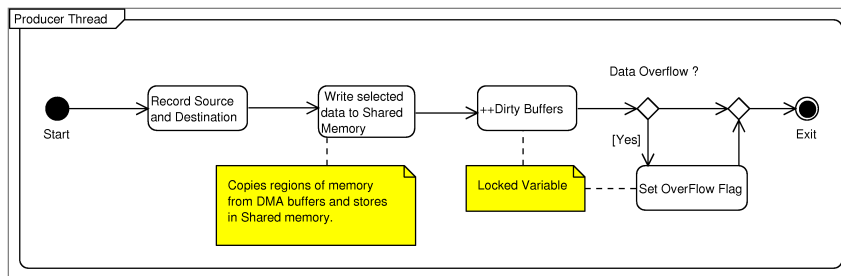


Figure 2.24: Producer Activity Diagram

at the observatory select portions of data, called windows, from the possible selection of data. Currently, this feature is handled in software, requiring no additional computation but increases data rates across the PCI bus. In the configuration program discussed in Chapter xxx, three windows: 1) TX window, 2) Data window, and 3) the Noise window, were chosen from the total number of samples collected in one IPP. Data selection takes place when data is transferred from the DMA buffers into the Shared buffers. The

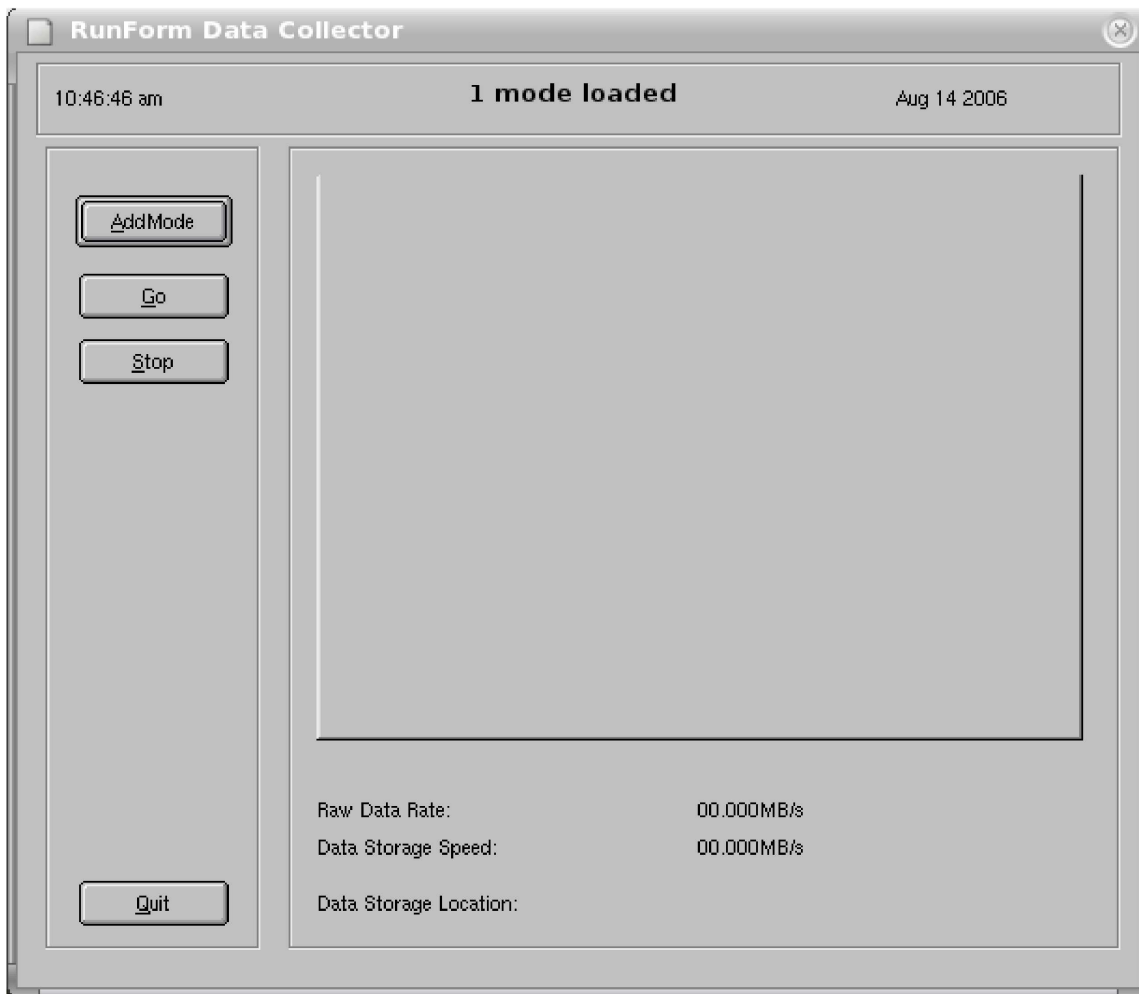


Figure 2.25: Run Time GUI

Run-Time graphical interface is depicted in 2.25 and provides a simple, direct interface for loading preconfigured modes into memory. The system indicates system status and incoming system data rates. Time and date are also displayed along with the number of modes loaded into memory. The center frame will eventually be used to display details of the current running mode e.g. experiment description, bandwidth, number of channels used, etc.. .

2.4 Real-Time Data Display

One drawback of an IF digital sampling system is the difficulty that arises when trying to verify data as it passes through the processing chain. The GC214 passes data via the PCI bus into the PC's RAM. One benefit of using shared memory is the ability to access data real-time using a separate process. Operation of the real-time data display uses this principle and is capable of displaying raw voltage in the time-domain as well as data in the frequency domain. Since data is stored in one-second buffers, the data display updates at a rate of 1 Hz. To compute FFT's efficiently, the Fastest Fourier Transform in the West (FFTW) was used to compute an adjustable N-point complex transform.

2.5 Data Format and Storage

Data storage requires a well defined format enabling many users to process data using a variety of languages. Scientific data commonly uses a format including *headers*, or tags used to describe a blocks of data. A number of formats are in use today; the most common of these being NASA's FITS and the NCSA's HDF formats. After a careful study of the FITS format, it was decided that, in order to achieve required efficiency and speed, a custom format would be needed. This custom format is labeled the Simple Header System (SHS) due to its quick, efficient implementation. Since the design was custom, an important goal was to provide a balance between readability and efficiency. In this section a description of the system will be given along with the C++ library resulting from the initial development.

File Name

Simple Header files (SHS), are defined by the .shs extension, and a data set consists of multiple files sharing a common basename and an increasing index number starting from 000. A sample data set is depicted in ??.

```
1 testFile_000.shs
2 testFile_001.shs
3 testFile_002.shs
4 testFile_003.shs
5 testFile_004.shs
6 testFile_005.shs
7 testFile_006.shs
8 testFile_007.shs
```

Keyword

The purpose of the SHS structure is to fully describe all aspects of the data so that, upon retrieval, all variables required for processing are available. Variables are described using keywords. A keyword consists of four parts: (1) Name (2) Value (3) Type, and (4) Comment. All keywords and delimiters in the SHS file are 96 bytes in length and are in ASCII format. This provides negligible overhead and serves two important purposes:

1. The primary and first data header (described below) can be examined using command line tools (more,less,etc...). This provides a quick method for verification without the need for specialized software.
2. Using ASCII for header information removes byte ordering dependence. This simplifies header parsing when working with multiple platforms.

File Structure

Each SHS file consists of 3 primary structures:

1. Primary Header

This header is located at the beginning of each file in a data set. The information is static and both fixed and custom keywords are present.

2. Data Header

The data header precedes every data table in a file and describes dynamic information relevant to the table that follows. Multiple data tables exist in a single file.

3. Data Table

Data Tables are blocks of data with a size defined by the user. Block size usually corresponds to a particular boundary preferable for processing. Tables can be formatted in either ASCII or binary.

A visual summary is shown in Figure 2.26 and a complete description is given in the SHS Headers section of this document. Each SHS file begins with a title, version, and author section; followed by the license. This section is referred to as the file ID and provides a method for verifying the file type and version of software used to create the file. Figure 2.27 illustrates the current file ID.

SHS Headers

SHS files contain two types of headers: 1) primary header and 2) data header. Together, these headers fully describe both static and dynamic information related to the stored data. Each header uses keywords to describe data and each follow a structured format

SHS File Layout

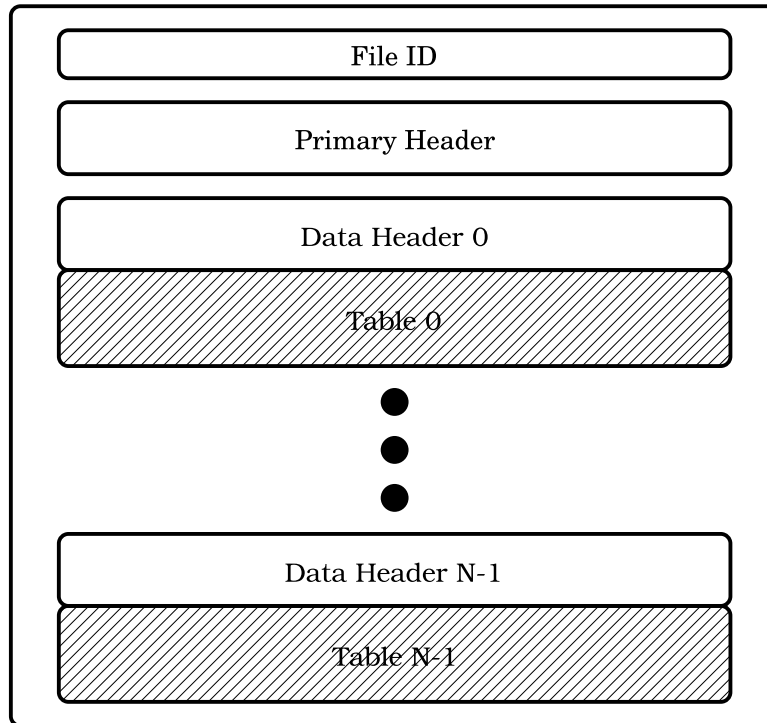


Figure 2.26: SHS Layout

Simple Header System version: 0.01 author: Ryan Seal <rseal@naic.edu>
 Copyright (C) 2005 GNU General Public License

Figure 2.27: SHS File ID

as shown in Figure 2.28: There are two types of keywords used in SHS files. Figure

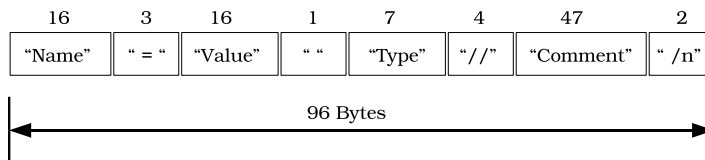


Figure 2.28: Keyword format

2.28 represents the most commonly used and the only custom configurable keyword. The other type of keyword belongs to a small part of the primary header and will be discussed in the following section.

Primary Header Format

The purpose of the Primary Header is to allow the user to document general information about the setup and configuration of the data set. This includes any information that will remain static throughout the data set; therefore, the header can be created before data acquisition and the header will remain consistent throughout the data set. In addition, a number of fixed keywords exist to describe internals of the file's structure. These keywords differ slightly from the previously mentioned standard. Specifically, they contain only a *name* and *value* but maintain the necessary 96-byte boundary. This format is shown below in Figure 2.29. All primary headers begin with four fixed keywords followed by

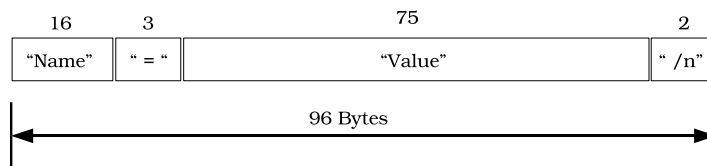


Figure 2.29: Keyword format

user-defined keywords as illustrated in the sample primary header below. Note that two of these fixed keywords are defined by the user. The remaining two describe the header type and the byte ordering of the system used to create the file.

```

1 Simple Header System          version: 0.02          author: Ryan Seal <rseal@naic.edu>
2 Copyright (C) 2005 GNU General Public License
3
4 HEADER:           = PRIMARY
5 TITLE:           = Echotek Data Col
6 DESCRIPTION:     = Echotek GC214-PC
7 BYTEORDER:      = LITTLE_ENDIAN
8 KEYWORDS:
9 [
10 FILENAME         = testFile           string // file name
11 DATE             = 04/13/2006         string // config create date
12 TIME             = 10:31:22 AST        string // creation time
13 ORIGIN           = Arecibo Observat    string // origin of data
14 OBSERVER         = RSEAL              string // observer
15 OBJECT           = Nothing            string // what is being observed
16 TELESCOPE        = NA                 string // telescope used
17 INSTRUMENT       = NA                 string // data collecting instrument
18 BWMODE           = Narrow             string // bandwidth mode
19 CHUSED           = 23                 string // number of channels used
20 COLMODE          = Burst              string // collection mode
21 GATESRC          = SIA                string // trigger source
22 GATEPLR          = RISING             string // trigger polarity
23 BURSTCOUNTER     = 17800             string // burst counter
24 DELAYCOUNT     = 0                  string // delay counter
25 SYNC            = SIA-COHERENT        string // synchronization
26 DATAFORMAT      = 16-bit complex     string // data format
27 CLOCKRATE        = 80                 string // clock frequency MHz
28 DECIMATION       = 20                 string // total system decimation
29 OUTPUTRATE       = 4                  string // system output rate
30 NCO1             = 24.5                double // NCO1 frequency MHz
31 NCO2             = 35.8                double // NCO2 frequency MHz
32 NCO3             = 0                  int    // NCO3 frequency MHz
33 NCO4             = 0                  int    // NCO4 frequency MHz
34 RESAMPLER        = OFF                string // resampler
35 IPP              = 10                 int    // IPP in msec
36 ]

```

A variable number of custom keywords can exist. Special delimiters are used to search and determine this number. The custom keyword section begins with a 'KEYWORDS:'

label and an opening '[' brace. Following the standard, the label and delimiter occupy 192 (2*96) bytes. The opening brace is followed by a number of keywords, each 96-bytes in length, and ends with a closing brace ']'; also 96-bytes. All 96-byte entities end with a newline character '\n', which occupies the 96th byte. The addition of the newline character allows the user to read a line of data (token) using predefined functions found in most common programming languages. Combining the braces with the fixed keyword size, the software can be designed so that keyword additions will be transparent.

2.5.1 Data Header Format

Data is written to the SHS file using a size determined by the user. Typically, this size is chosen to partition the data in a way that will enhance later processing. For example, if the user performs integrations with a resolution of 1 second; a one second block of data would be preferable. Data headers are used to describe these blocks of data. Again, fixed keywords are used to describe information about the structure of the data; but these keywords follow the standard format described earlier. Looking at the figure below, all keywords preceding the identifier 'KEYWORDS:' represent fixed keywords; which are required internally by the system. It should be noted that data can be stored in either ASCII or Binary tables. Custom keywords follow the fixed keywords in the exact manner as the primary header. A complete sample header is illustrated in Listing below:

```

1
2 HEADER:           = Binary           string // data storage format
3 TABLENUM:       = 0                 string // table number in current file
4 TABLESIZE:      = 6444000           string // table size with units of DATATYPE
5 DATAWIDTH:      = 2                 string // number of bytes in DATATYPE
6 DATATYPE:        = short             string // data type
7 NUMDIMS:         = 2                 string // number of dimensions

```

```

8 Dim0:           = 32220           int    // Dimension Number 0
9 Dim1:           = 200            int    // Dimension Number 1
10 KEYWORDS:
11 [
12 NUMCHANNELS    = 2              int    // number of channels
13 TX START       = 0              int    // TX start (DATATYPE)
14 TX SIZE        = 5200           int    // TX size (DATATYPE)
15 DATA START    = 6000           int    // DATA start (DATATYPE)
16 DATA SIZE     = 27000          int    // DATA samples (DATATYPE)
17 NOISE START    = 33000          int    // NOISE start (DATATYPE)
18 NOISE SIZE     = 20             int    // NOISE size (DATATYPE)
19 DATE           = 0              int    // date format YYYYDDD
20 SYSTIME        = time           string // current system time (AST)
21 AZIMUTH        = 0              float  // azimuth (DEG)
22 GREGPOS        = 0              float  // gregorian (DEG)
23 CARRPOS        = 0              float  // carriage house (DEG)
24 ]

```

Each data header begins with a 96-byte space delimiter. This provides a boundary between the data table and the next data available data header. The size of each file, by default, is approximately 2 GigaBytes (GB); allowing for compatibility across the spectrum of file systems. This 2 GB boundary is aligned to the data table's size; removing the need to deal with data tables that cross the file boundary. If required, the file size can be changed to any arbitrary size. Once the data table size has been chosen, it should remain consistent throughout the data set. If a user acquires data with different parameters, then these differences should be sorted and multiple data sets should be used. This greatly reduces complexity and provides a clean interface for other users of the data. For example, if a single stream of data is processed in three different ways (looking at different aspects of a single data set), each of the three processed streams should be stored in three separate data sets. Otherwise, the user must skip around for the particular set of data of interest; increasing software complexity and processing time.

Chapter 3

Radar Observations

In this chapter we present two radar experiments that utilized the new data acquisition system discussed earlier. Superb quality data acquired with this system attest its sensitivity and for its class of modern DAS for research radars.

3.1 Meteor Observations

High power and large aperture (HPLA) radars designed for incoherent scattering sensing of the ionosphere can detect decelerating particles in the size range 0.5-500 mm, smaller than those detected by conventional meteor radars, allowing one to study a mass region of the interplanetary dust distribution that was previously inaccessible to ground-based instruments, and help to bridge the gap between spacecraft dust measurements and traditional meteor radar capabilities. In addition, the high sensitivity of the new DAS system provides very large sets offering unprecedented statistics for this particle mass range.

In this section, a technique for real-time meteor detection is described and analysis of two parameters: 1) height, and 2) radial velocity from a single event, recorded on

March 04, 2006, will be shown. In this particular experiment, meteor observations were conducted in the E-region of the ionosphere using 47 μ s uncoded pulses. The IPP was 2 ms and 4000 ranges were sampled at 37.5 m intervals starting at 77 km range. The radar operated with a maximum peak power of about 1.6 MW. This meteor data was formatted and stored using the Simple Header System described in Section 2.5. The received signal of the radar was stored in binary format using 16-bit In-phase (I) and 16-bit Quadrature (Q) samples. A detection algorithm was used offline to find and isolate meteor events for the entire data set.

3.1.1 Detection Algorithm

The system's ADCs accept a maximum input of 1 V_{p-p} into a 50 Ohm load (4dBm). Voltage is produced from the digitized samples as

$$\tilde{v}[n] \equiv \tilde{s}[n] \frac{V_{range}}{2^b} = \frac{\tilde{s}[n]}{65536}, \quad (3.1)$$

where $\tilde{s}[n]$ is the complex, digitized data sample, V_{range} is 1 V_{p-p} , and b is 16 bits. Next, power (RMS) is computed from the complex samples

$$P[n] \equiv \left| \frac{\tilde{v}[n]}{\sqrt{2}R} \right|^2 \equiv \frac{\tilde{v}[n]\tilde{v}[n]^*}{2R^2} = \frac{Re\{\tilde{v}[n]\}^2 + Im\{\tilde{v}[n]\}^2}{500}. \quad (3.2)$$

To reduce noise contamination, a moving-average filter is implemented and detection is maximized by setting the sample average equal to the width of the transmitted pulse

$$y[n] = \sum_{k=0}^{K-1} P[n+k] \quad \text{for } 0 \leq n \leq N-1, \quad (3.3)$$

where K is the length of the transmitted pulse and N is the total number of samples. This operation is essentially a cross-correlation of the received signal with the normalized transmitter pulse. For efficiency, the filter is implemented recursively beginning with computation of the initial value

$$y[0] = \sum_{k=0}^{K-1} P[k].$$

Remaining computations are reduced to

$$y[n] = y[n - 1] + P[n + K] - P[n - 1] \quad \text{for } 1 \leq n \leq N - 1.$$

Next, a fast-time (1 IPP) noise estimate is determined by

$$\hat{P}_n = \frac{1}{N - M} \sum_{n=M}^{N-1} P[n], \quad (3.4)$$

where M is the starting height and N is the final height used in the estimation. The filtered signal and a scaled noise estimate are used to determine detection

$$y[n] > \alpha \hat{P}_n, \quad (3.5)$$

where α is the threshold value. This process is repeated for each IPP.

3.1.2 Parameter Estimation

To verify system operation, a number of events were recorded simultaneously with the current system. Two parameters, height and velocity, were processed using the new DAS and verified with the current system. In this section, a discussion of the method used for processing will be given using a single event detected on March 04, 2006.

Each table of data stored using the SHS file system contains one second of data. Using an IPP of 2 *ms*, 500 IPPs are available per table. The Range Time Intensity (RTI) plot displays range and IPP number in the x-y directions and power is displayed using a color map. Figure 3.1 illustrates an RTI plot of an event at 4:10:01 AST. From the image in

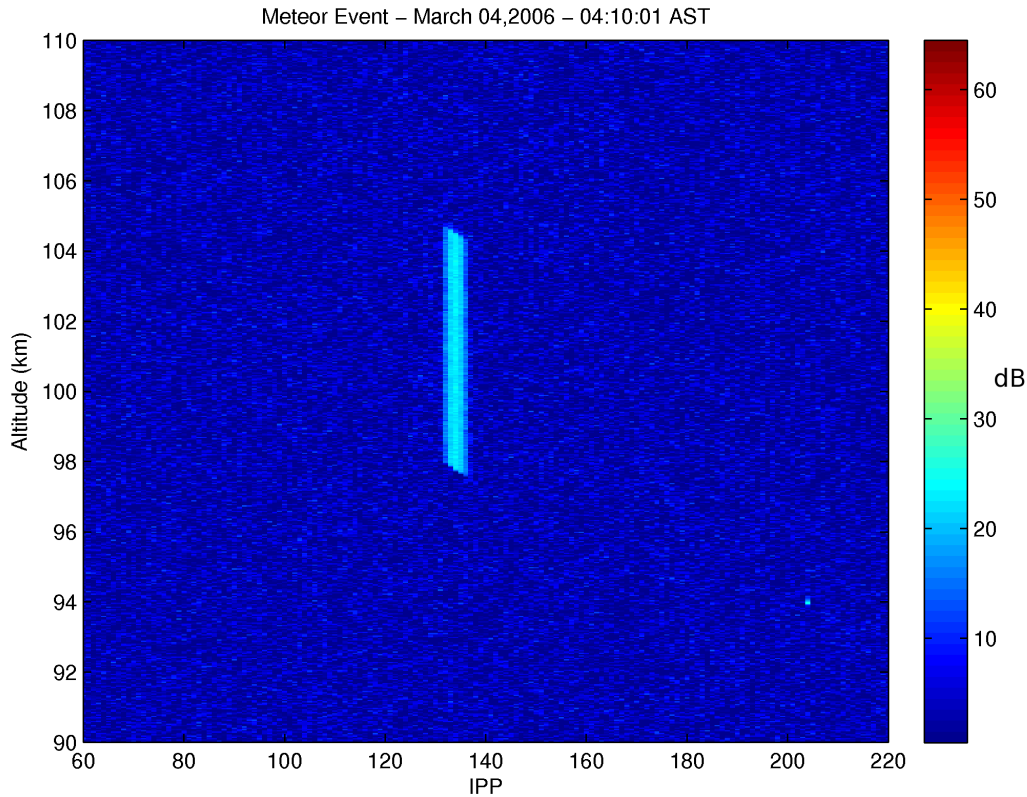


Figure 3.1: Range Time Intensity (RTI) plot

Figure 3.1, a single IPP is isolated from the data and plotted in Figure 3.2. This figure provides enough information to compute both range and velocity of the meteor. In this example, steps taken to process this information are automated using MATLAB software and details are located in B.1. First, power from the radar return is computed for a single IPP and is illustrated in Figure 3.3. Second, a cross-correlation of the power signal with

power from the transmitted pulse are computed. The result will produce a waveform as shown in Figure 3.4. The peak of this waveform provides the midpoint of the meteor's range and is used to isolate the event for further processing. Isolation of the detected event is shown in Figure 3.5. Next, an FFT analysis is performed on the isolated event and the results are normalized as shown in Figure 3.6. The spectrum's peak is used to calculate the meteor's radial velocity using

$$v = f_d \frac{\lambda}{2}, \quad (3.6)$$

where v represents radial velocity (m/s), f_d is the spectrum peak, and λ is the wavelength of the transmitted carrier (m). The following results were processed and verified with the current system:

1. Range: 97.039 km \pm 18.74 m

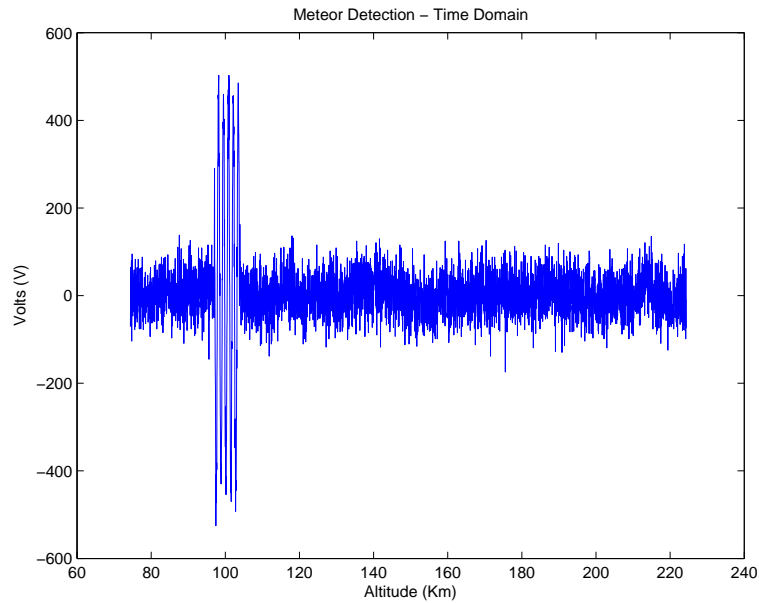


Figure 3.2: IPP illustrating meteor in time domain

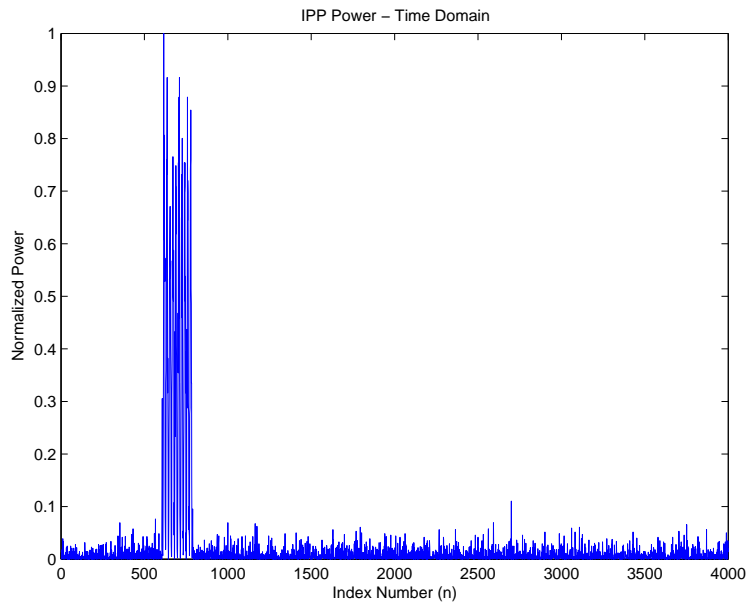


Figure 3.3: IPP power computation

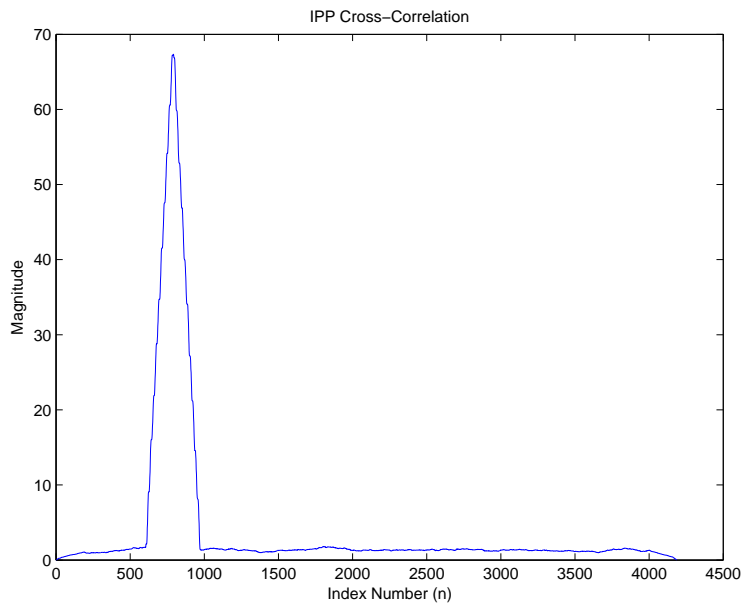


Figure 3.4: IPP cross-correlation with transmitted power to isolate detection

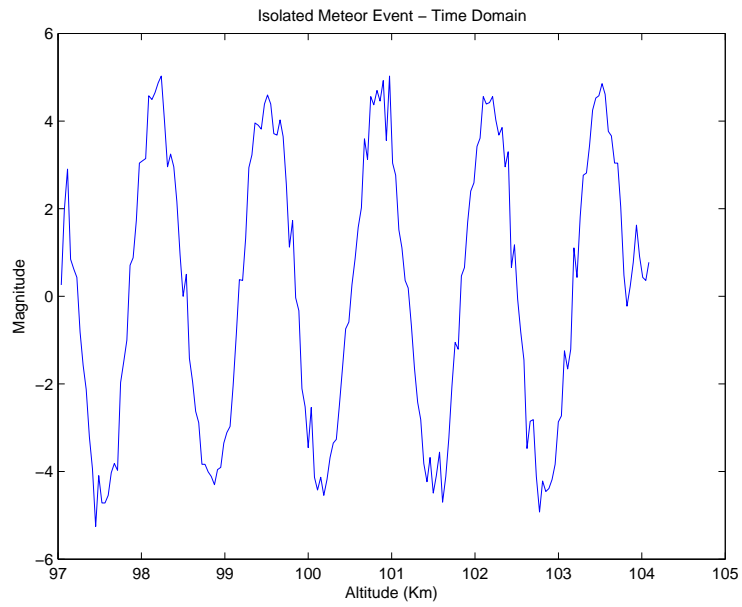


Figure 3.5: Isolated Meteor detection resulting from cross-correlation

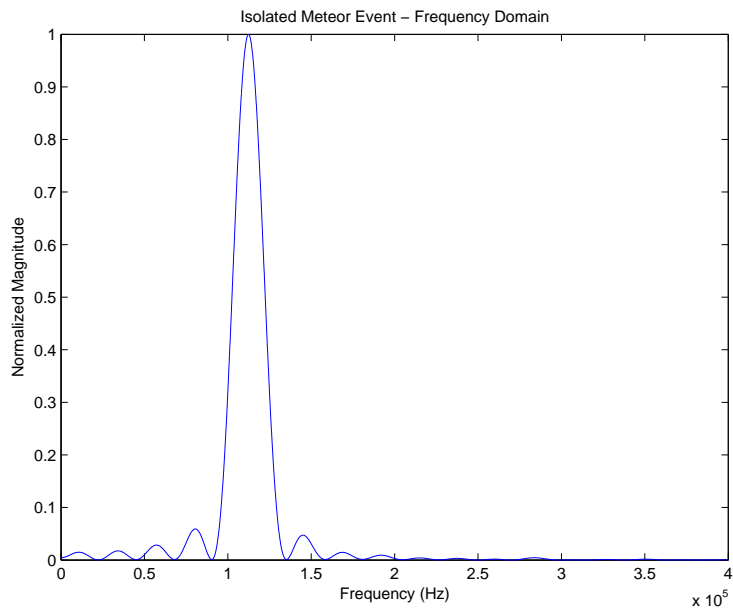


Figure 3.6: Spectrum from meteor detection illustrating doppler spectrum

2. Velocity: $39.219 \text{ km/s} \pm 61.04 \text{ m/s}$

Error estimation of range was based on the system's sampling rate (4 MHz) and velocity error was calculated using both sampling rate and the number of points (32k) used in the FFT analysis. Events from the current system were processed and a comparison revealed precise matching, thus verifying system operation.

3.2 Plasma Line Observations

It is well-known that the most accurate method for measuring the electron density in the upper atmosphere is using the plasma line resonance, which occurs close to the plasma line frequency as predicted by incoherent scatter (IS) theory [e.g., Dougherty and Farley, 1960; Salpeter, 1960]. The plasma line (caused by scattering from electron plasma waves) is greatly enhanced over thermal levels during the daytime by photo electrons [e.g., Yngvesson and Perkins, 1968]. The information in the plasma line resonance lies in the frequency of the return, not in the shape of the spectrum, as is the case for the ion line. Frequency measurements are much more accurate than power or amplitude measurements since they do not depend on receiver gains and system losses, which are often difficult to measure and quite variable. Thus, using the plasma line resonance frequency as an ionospheric diagnostic is particularly useful.

In this section, we present the first results of a new technique for measuring the electron temperature in the daytime ionosphere using the Arecibo incoherent scatter radar (ISR). The technique utilizes the plasma line component of the incoherent scatter spectrum. The difference in the up- and down-shifted plasma line frequencies is related to the density and temperature of the ionosphere, as well as more minor effects resulting from photoelectrons, currents, and other sources. The shift is very small (the order of

1 kHz in a plasma line frequency of several MHz) but can be measured quite accurately with the coded long pulse plasma line technique. We compare the results to ion line measurements of the electron temperature, and the two independent techniques show good agreement. In addition to providing a measure of the electron temperature that is independent of the ion line, the approach allows for a sensitive test of kinetic plasma theory including a magnetic field, gives us the ability to study photoelectron populations and electron currents, and will allow us to constrain ion line fits in the bottomside (and possibly topside) regions to more accurately fit for composition.

Chapter 4

Conclusions and Future Work

It is clear that the new DAS for the Arecibo radar has the capability of measuring high quality data as attested by both meteor and plasma radar observations. The flexibility and reliability of the system allows visiting scientists to develop exciting experiments in space science.

We plan to enhance data throughput, system flexibility and capabilities by including Field Programmable Gate Arrays (FPGA) technology at the front-end of the data acquisition system and utilized a USB port for system control and communication. Of course segments of the software presented in this thesis will have to be modified and adapted in order to integrate this FPGA system. Also, the integration of a radar controller with the data acquisition system will be conducted.

Finally, the radar software and control programs developed under this project will be available freely to anybody through the Open Source software development web site of SourceForge at: [<http://sourceforge.net>].

Appendix

A Convolution Sum Derivation

Derivation of the convolution sum begins with definition of the unit sample sequence

$$\delta(n) = \begin{cases} 1 & n = 0 \\ 0 & n \neq 0. \end{cases} \quad (1)$$

Using properties of the unit sample sequence, an alternative input sequence is given by

$$x[n] = \sum_{k=-\infty}^{\infty} x[k]\delta[n - k]. \quad (2)$$

Substituting Equation (2) into Equation (1.20) results in

$$y[n] = \tau \left[\sum_{k=-\infty}^{\infty} x[k]\delta[n - k] \right]. \quad (3)$$

Applying the property of linearity to equation (3)

$$y[n] = \sum_{k=-\infty}^{\infty} x[k]\tau \left[\delta[n - k] \right]. \quad (4)$$

Equation (4) contains another important sequence known as the unit impulse response

$$h[n, k] = \tau \left[\delta[n - k] \right]. \quad (5)$$

Applying the property of time-invariance to equation (5) results in

$$h[n - k] = \tau \left[\delta[n - k] \right]. \quad (6)$$

Combining the previous work into a single equation, a resulting output sequence

$$y[n] = \sum_{k=-\infty}^{\infty} x[k]h[n - k] \quad (7)$$

defines the output response in terms of both the input sequence and impulse response of the system. The form of equation (7) is known as the convolution sum and is widely used in the analysis and development of DSP algorithms.

B MATLAB Programs

B.1 metFreq.m

```
1 function [x,xfft,pfft,freq,time,F1,fftPoints,velocity,pulse]=
2     metFreq(fileName, sampleRate, pulseWidth)
3
4 %32k-point FFT
5 fftPoints = 1024*32;
6
7 %number of samples in tx pulse
8 pulse=ones(1,pulseWidth*sampleRate);
9
10 %ascii file containing detected IPP
11 x = load(fileName);
```

```

12
13 %isolate data window from IPP
14 orig = x(401:4400);
15 x = x(401:4400);
16
17 %compute pwr
18 xpwr = x.^2;
19 xpwr = xpwr/max(xpwr);
20
21 %cross-correlate signal with pulse
22 detection = conv(xpwr,pulse);
23
24 %find max point from correlation
25 [detection,index] = max(detection);
26
27 %treat max as midpoint and isolate detected samples from the IPP
28 %adjust for cross-correlation length
29 h1 = index - length(pulse);
30 h2 = index;
31
32 %starting height with cabling delay adjustment (4us)
33 h0 = sampleRate^-1*2000/6.67e-6 - 4/6.67;
34
35 %sample step in Km
36 tStep = 250e-9/6.67e-6;
37
38 %create altitude axis
39 axis1 = 1:4000;
40 axis1 = axis1*tStep+h0;
41
42 %compute one-sided spectrum
43 xfft = fft(x(h1:h2),fftPoints);
44 pfft = xfft .* conj(xfft);
45 pfft = pfft(1:length(pfft)/2);
46
47 %create frequency axis
48 freq = 0:sampleRate/fftPoints:sampleRate/2-1;
49
50 %plot data window
51 subplot(3,1,1);

```

```

52 plot(axis1,orig);
53
54 %plot detection window
55 subplot(3,1,2);
56 plot(axis1(h1:h2),x(h1:h2));
57
58 %plot normalized spectrum
59 subplot(3,1,3);
60 pfft = pfft / max(pfft);
61 plot(freq,pfft);
62
63 %search for spectrum max
64 for i=1:length(pfft)
65     if(pfft(i)==1) maxPoint = i;
66     end
67 end
68
69 %compute radial velocity from doppler spectrum
70 velocity = (freq(maxPoint)/2)*(3e8/430e6)
71 hDetect = axis1(h1)
72 error = sampleRate/fftPoints
73 %\end{lstlisting}

```

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